

希尔伯特空间浅述 – 兼谈从工程的角度看数学

An Introduction to L^2 Space
- An Engineering's View of
Mathematics

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数学是自然现象和社会现象包括工程技术的高度概括和抽象描述。本学术报告以泛函分析中的一个比较难理解的数学概念，**希尔伯特空间**为例，从工程的角度给出了形象的，比较好理解的描述。**将抽象的数学还原为实际的工程问题**。此报告还介绍了有关希尔伯特空间理论在模式识别中的应用实例。

此报告通俗易懂，通过形象的比喻加深听众对数学理论的理解，为工程技术人员更好地应用数学理论以及数学家如何将数学理论和实际应用相结合提供帮助。

此为作者在国家基金委信息科学部所作报告的讲稿整理修改而成，和大家分享。

“Access to wavelet theory has been limited because much of the wavelet literature requires that the reader understand the **mathematics** of functional analysis 泛函分析 Hilbert space theory 希尔伯特空间

1 An Overview

“Wavelets” has been a very popular topic of conversations in many scientific and engineering gatherings these days. Some view wavelets as a new basis for representing functions, some consider it as a technique for time-frequency analysis, and others think of it as a new mathematical subject. Of course, all of them are right, since “wavelets” is a versatile tool with very rich mathematical content and great potential for applications. However, as this subject is still in the midst of rapid development, it is definitely too early to give a unified presentation. The objective of this book is very modest: it is intended to be used as a textbook for an introductory one-semester course on “wavelet analysis” for upper-division undergraduate or beginning graduate mathematics and engineering students, and is also written for both mathematicians and engineers who wish to learn about the subject. For the specialists, this volume is suitable as complementary reading to the more advanced monographs, such as the two volumes of *Ondelettes et Opérateurs* by Yves Meyer, the edited volume of *Wavelets-A Tutorial in Theory and Applications* in this series, and the CBMS volume by Ingrid Daubechies.

$L^2(0, 2\pi)$

Wavelet analysis is a relatively new subject and the approach and in this book are somewhat different from that in the others, the chapter is to convey a general idea of what wavelet analysis is about and what this book aims to cover.

1.1. From Fourier analysis to wavelet analysis

Let $L^2(0, 2\pi)$ denote the collection of all measurable functions f defined on the interval $(0, 2\pi)$ with

$$\int_0^{2\pi} |f(x)|^2 dx < \infty.$$

For the reader who is not familiar with the basic Lebesgue theory, the sacrifice is very minimal by assuming that f is a piecewise continuous function. It will always be assumed that functions in $L^2(0, 2\pi)$ are extended periodically to the real line

$$\mathbf{R} := (-\infty, \infty),$$

namely: $f(x) = f(x - 2\pi)$ for all x . Hence, the collection $L^2(0, 2\pi)$ is often called the space of 2π -periodic square-integrable functions. That $L^2(0, 2\pi)$ is

1

2

1. An Overview

a vector space can be verified very easily. Any f in $L^2(0, 2\pi)$ has a Fourier series representation:

$$f(x) = \sum_{n=-\infty}^{\infty} c_n e^{inx}, \quad (1.1.1)$$

where the constants c_n , called the Fourier coefficients of f , are defined by

$$c_n = \frac{1}{2\pi} \int_0^{2\pi} f(x) e^{-inx} dx. \quad (1.1.2)$$

The convergence of the series in (1.1.1) is in $L^2(0, 2\pi)$, meaning that

$$\lim_{M, N \rightarrow \infty} \int_0^{2\pi} \left| f(x) - \sum_{n=-M}^N c_n e^{inx} \right|^2 dx = 0.$$

There are two distinct features in the Fourier series representation (1.1.1). First, we mention that f is decomposed into a sum of infinitely many mutually orthogonal components $g_n(x) := c_n e^{inx}$, where orthogonality means that

$$\langle g_m, g_n \rangle^* = 0, \quad \text{for all } m \neq n, \quad (1.1.3)$$

with the “inner product” in (1.1.3) being defined by

$$\langle g_m, g_n \rangle^* := \frac{1}{2\pi} \int_0^{2\pi} g_m(x) \overline{g_n(x)} dx. \quad (1.1.4)$$

That (1.1.3) holds is a consequence of the important, yet simple fact that

$$w_n(x) := e^{inx}, \quad n = \dots, -1, 0, 1, \dots, \quad (1.1.5)$$

is an orthonormal (o.n.) basis of $L^2(0, 2\pi)$. The second distinct feature of the Fourier series representation (1.1.1) is that the o.n. basis $\{w_n\}$ is generated by “dilation” of a single function

$$w(x) := e^{ix}; \quad (1.1.6)$$

that is, $w_n(x) = w(nx)$ for all integers n . This will be called *integral dilation*.

Let us summarize this remarkable fact by saying that every 2π -periodic square-integrable function is generated by a “superposition” of integral dilations of the basic function $w(x) = e^{ix}$.

We also remark that from the o.n. property of $\{w_n\}$, the Fourier series representation (1.1.1) also satisfies the so-called *Parseval Identity*:

$$\frac{1}{2\pi} \int_0^{2\pi} |f(x)|^2 dx = \sum_{n=-\infty}^{\infty} |c_n|^2. \quad (1.1.7)$$

崔景泰 Charles K. Chui, *An Introduction to Waves*, Academic Press, 1992

Linear Space
线性空间

Abstract Space
抽象空间

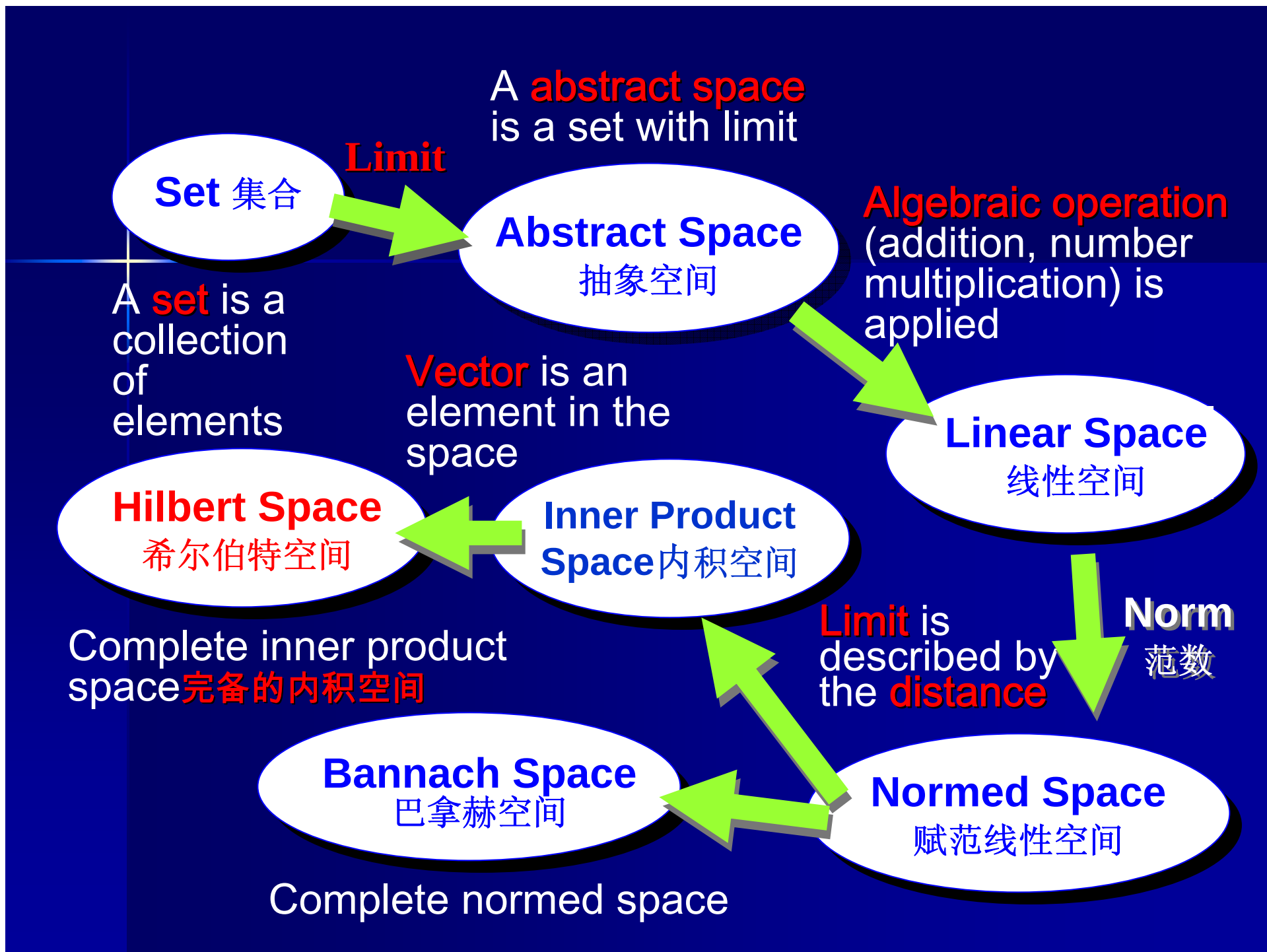
**Bannach
Space**

**Functional
Analysis**
泛函分析

Norm 范数

Hilbert Space

Normed Space
赋范空间



$L^2(\mathbb{R}^2)$ 空间的基本性质: (泛函分析)

└ 定义在 $\mathbb{R}^2$ 上的完备的内积空间.

内积: $\forall f, g \in L^2(\mathbb{R}^2)$, 对应一个实数 $\langle f, g \rangle$
(或复数)

$\langle f, g \rangle$ $\left\{ \begin{array}{ll} \text{非负性} & \langle f, f \rangle \geq 0 \\ \text{对称性} & \langle f, g \rangle = \langle g, f \rangle \\ \text{线性性} & \langle \alpha f + \beta g, h \rangle = \alpha \langle f, h \rangle + \beta \langle g, h \rangle \end{array} \right.$

完备：(对极限运算的封闭性)

- 自然数：对“+”封闭，对“-”不封闭
- 整数：+，-， $\times$ 封闭， $\div$ “ ”
- 有理数：(凡可表示为 $\frac{m}{n}$ 的数：整数、分数、有限或无限循环小数)
+，-， $\times$ ， $\div$ 封闭，对极限不封闭

例： $\pi = 3.1415926535932354626 \dots$ 是无理数
(山顶一寺一壶酒，尔乐吾煞吾，酒杀尔，杀不死，乐而乐)

完备: (对极限运算的封闭性)

例: $\pi = 3.1415926535932354626 \dots$ 是无理数
(山顶一寺一壶酒, 尔乐吾煞吾, 酒杀尔, 杀不死, 乐而乐)

考察 - 有理数的数列 $\{a_n\}$

$$a_1 = 3, a_2 = 3.1, a_3 = 3.14, \dots$$

$$\lim_{n \rightarrow \infty} a_n = \pi \quad \text{此极限不包括在有理数内}$$

• **实数**: (有理、无理统称)

$+$, $-$, $\times$, $\div$, 极限均封闭

L2(R²) 空间的函数 的重要性质

如果 $f(x,y)$ 是 $L^2(\mathbb{R}^2)$ 空间的函数, 即 $f(x,y) \in L^2(\mathbb{R}^2)$, 则 $f(x,y)$ 是平方可积函数, 即函数的能量有限

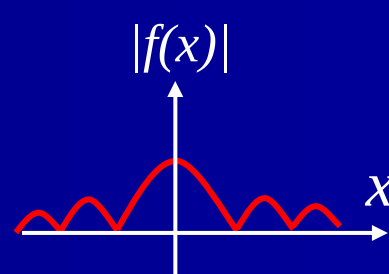
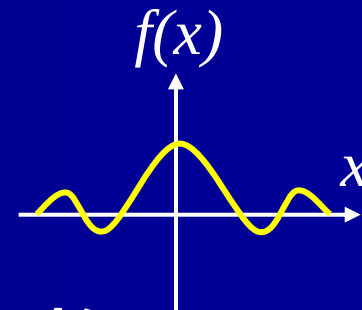
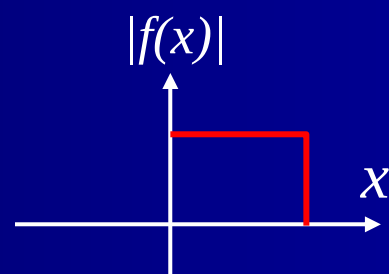
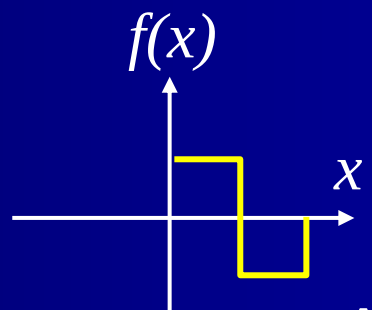
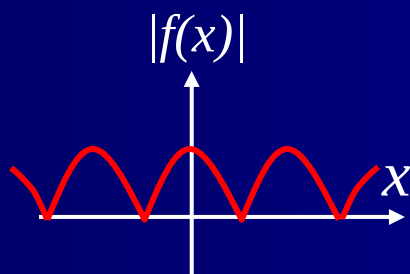
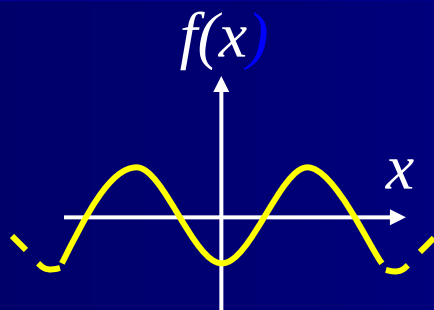
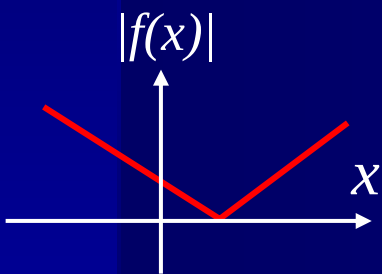
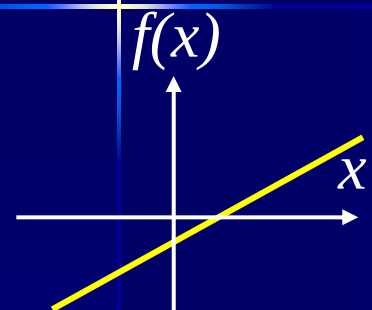
$$\iint_{\mathbb{R}^2} |f(x,y)|^2 dx dy < \infty$$

函数的能量

$$f(x) \in L^2(\mathbb{R})$$

$f(x)$ 是平方
可积函数

$$\int_{-\infty}^{\infty} |f(x)|^2 dt < \infty$$



小波函数

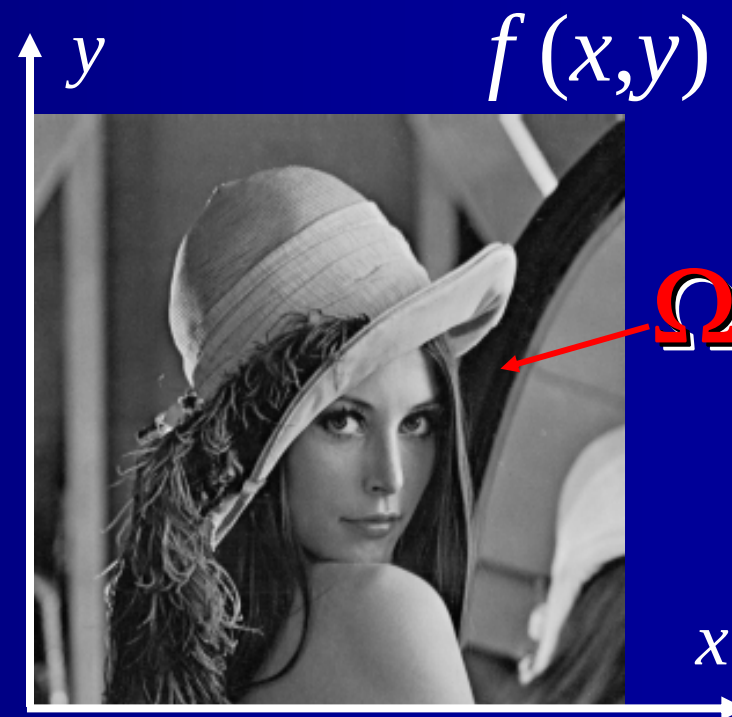
$$f(x,y) \in L^2(\mathbb{R}^2)$$

$$\longleftrightarrow \iint_{\mathbb{R}^2} |f(x,y)|^2 dx dy < \infty$$

f 是平方可积函数

图像是 $L^2(\mathbb{R}^2)$ 空间的函数

- 图像的面积是有限的: Ω
- 图像的像素灰度级是有限的: $0 \leq f(x,y) \leq 255$
- 所以



$$0 = \iint_{\Omega} 0 dx dy \leq \iint_{\Omega} |f(x,y)|^2 dx dy \leq \iint_{\Omega} 255^2 dx dy = 255^2 \Omega < \infty$$

图像是 $L^2(\mathbb{R}^2)$ 空间的函数

$$0 = \iint_{\Omega} 0 dx dy \leq \iint_{\Omega} |f(x, y)|^2 dx dy \leq \iint_{\Omega} 255^2 dx dy = 255^2 \Omega < \infty$$

- 这个公式仅仅考虑在图像面积 Ω 内的积分.
- 从数学的角度应该考虑在整个空间 $\mathbb{R}^2$ 内的积分
- 我们在整个空间 $\mathbb{R}^2$ 内制造一个新的图像

$$f(x, y) = \begin{cases} f(x, y) & (x, y) \in \Omega \\ 0 & (x, y) \notin \Omega \end{cases}$$

- 因此

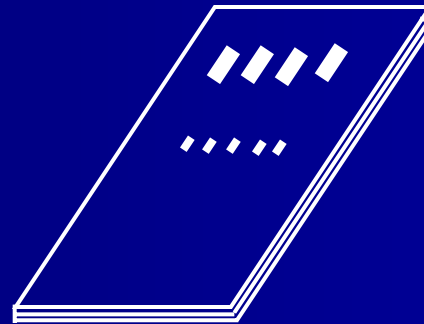
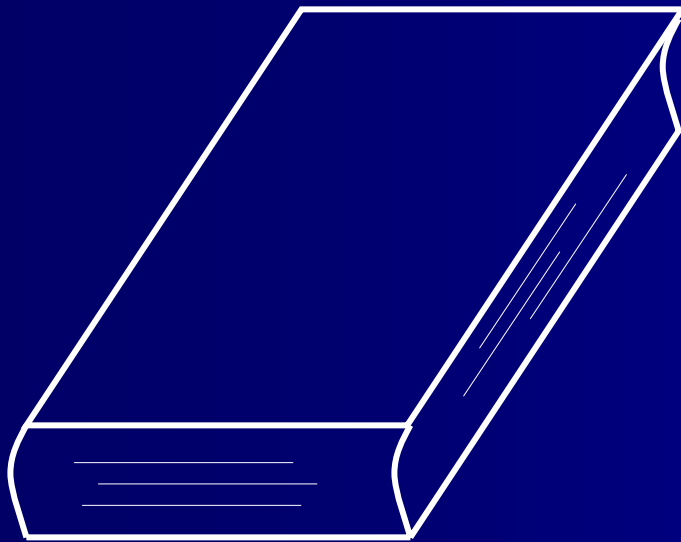
$$0 \leq \iint_{\mathbb{R}^2} |f(x, y)|^2 dx dy \leq 255^2 \Omega < \infty$$

**$L^2(\mathbb{R}^n)$ 空间的一类重要
函数 — 小波函数
(Wavelets)**

Waves, Wavelets, and Transforms 波、小波和变换

Waves & Wavelets 波和小波

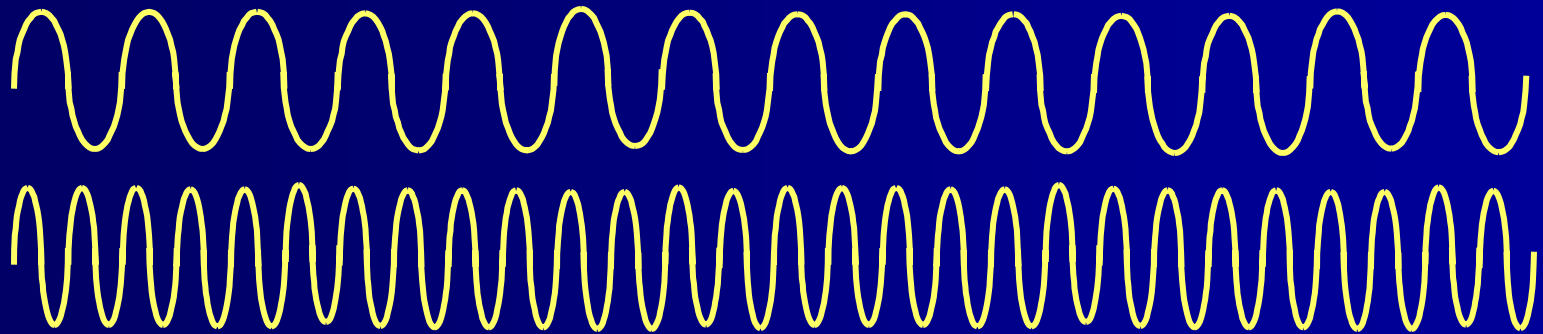
A new word in English - Wavelets



Book and booklet 书和小册子

Waves & Wavelets 波和小波

Waves 波



Wavelets 小波



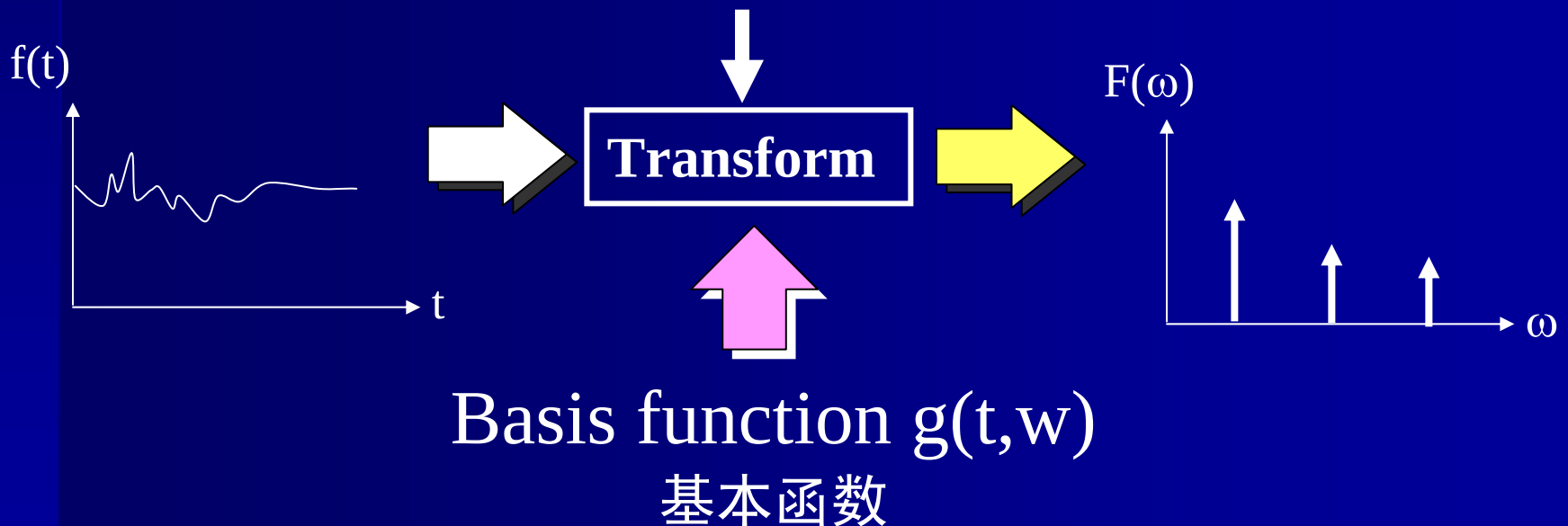
Transform 变换

Input function 被处理的信号

$$F(\omega) = \int_{-\infty}^{\infty} f(t)g(t, \omega) dt = \langle f(t), g(t, \omega) \rangle$$

Basis function 基本函数

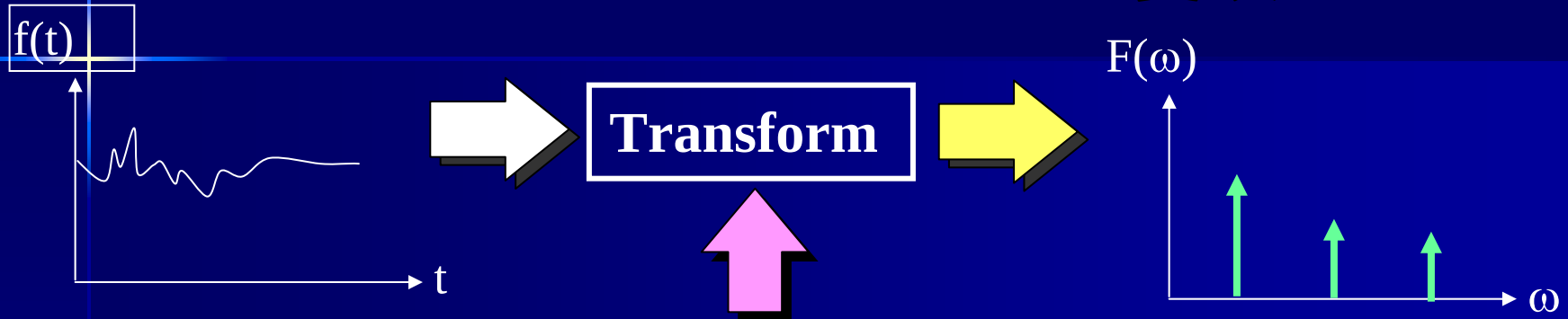
Operation:
Inner Product 内积



Wavelet Transform

小波

变换

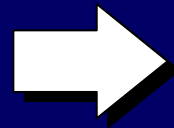


Basis function $g(t)$

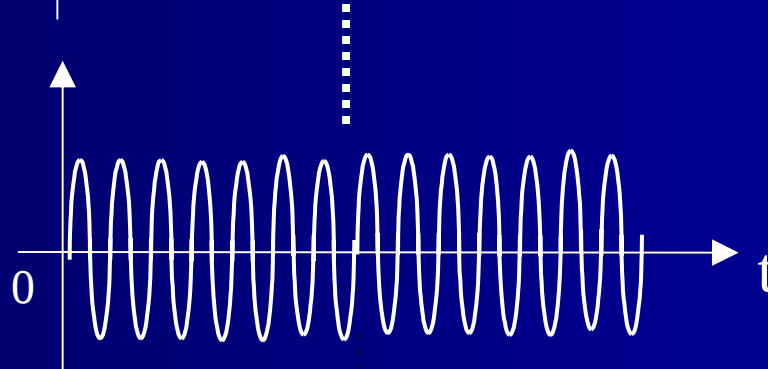
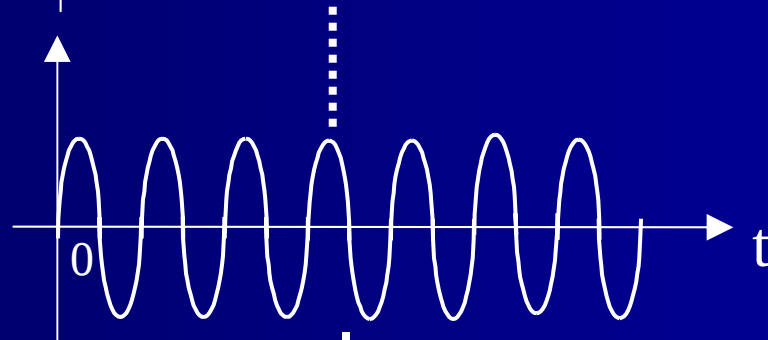
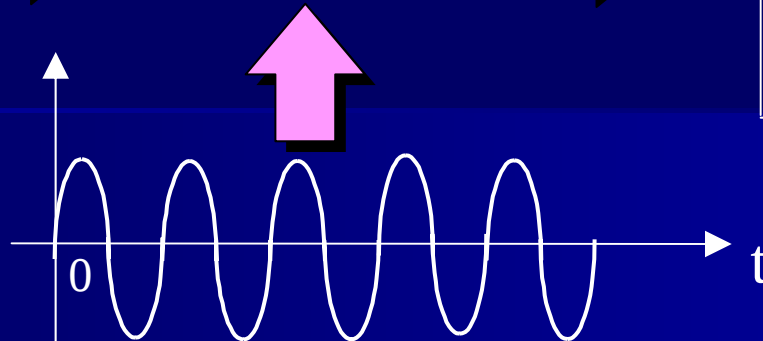
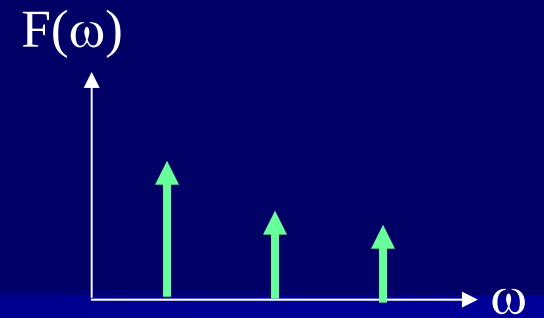
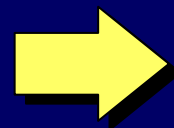
基本函数

**Wave
Function**
波函数

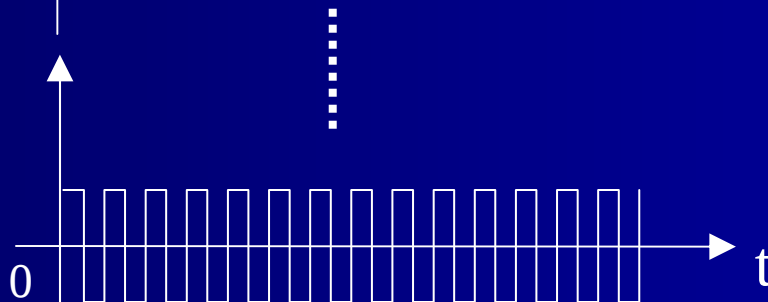
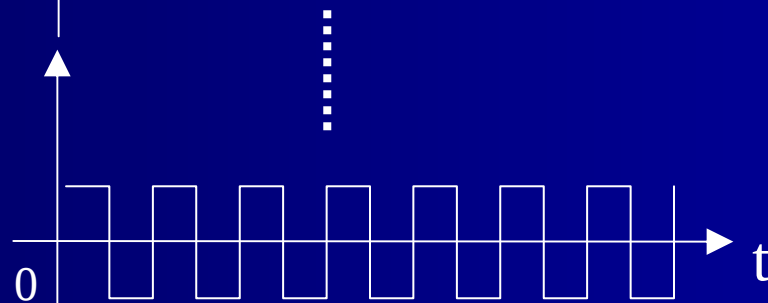
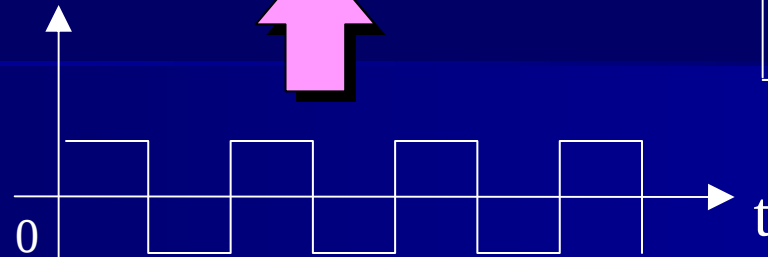
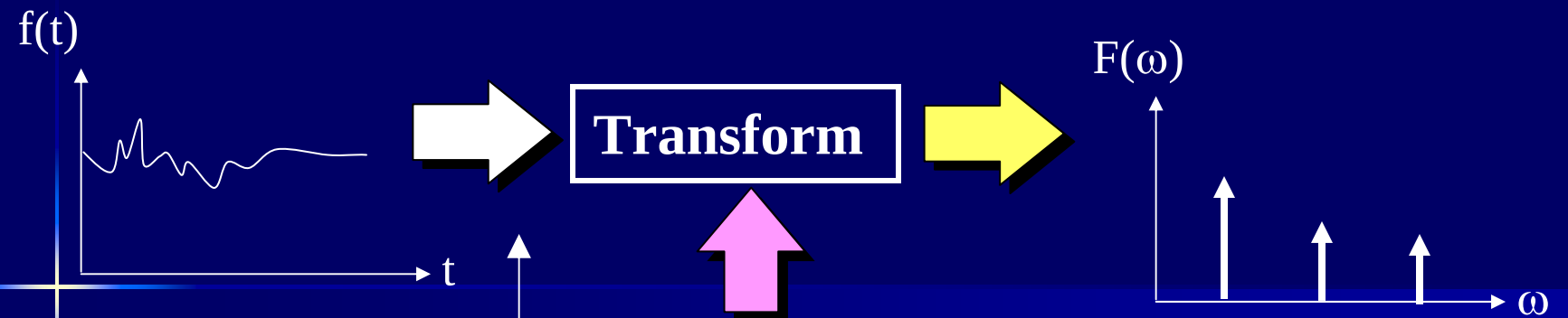
**Wavelet
Function**
小波函数



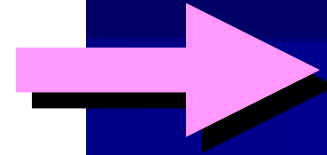
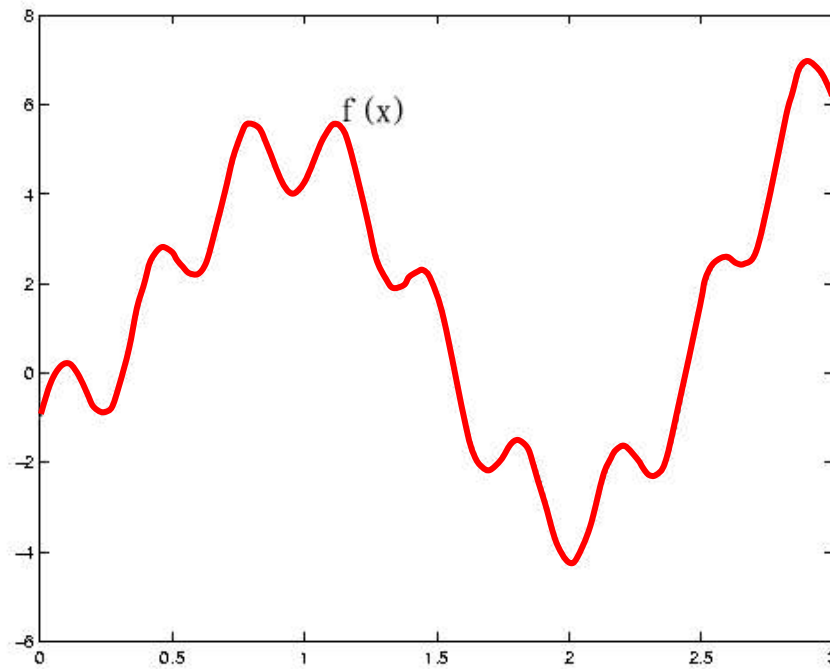
Transform



**Fourier
Transform**



**Walsh
Transform**



$$f(x) = f_0(x) + f_1(x) + 2 \times f_2(x) - 4 \times f_3(x) + f_4(x)$$

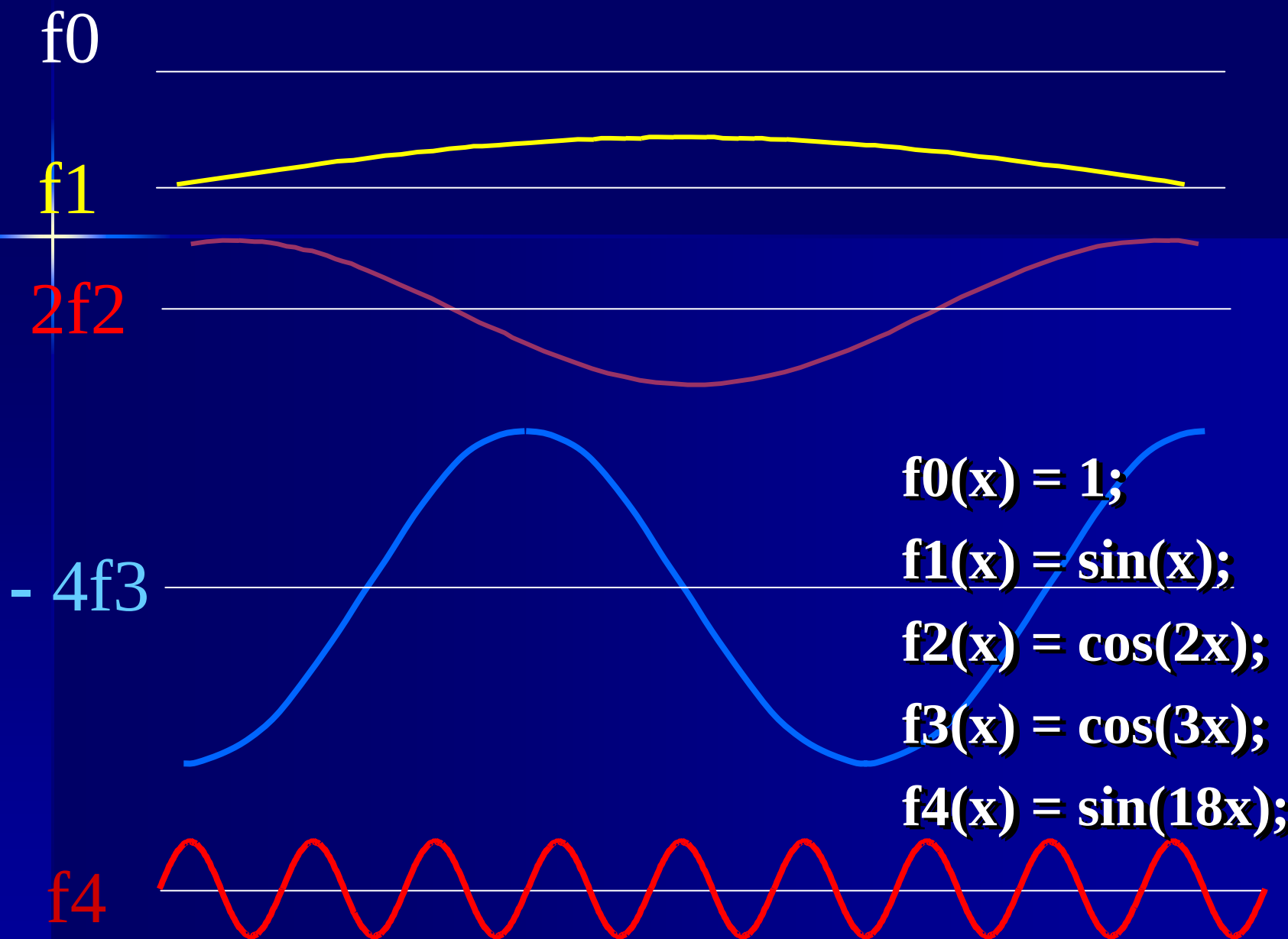
$$f_0(x) = 1;$$

$$f_1(x) = \sin(x);$$

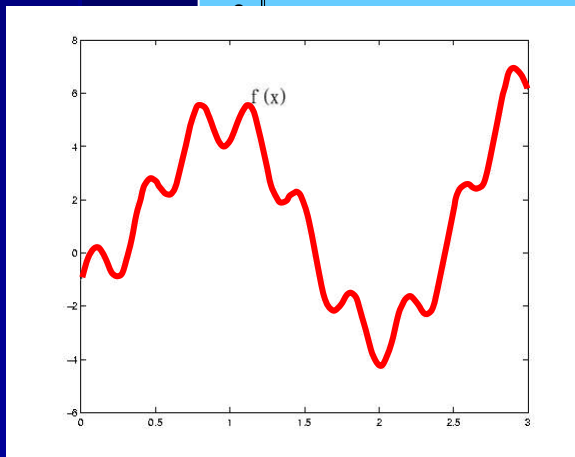
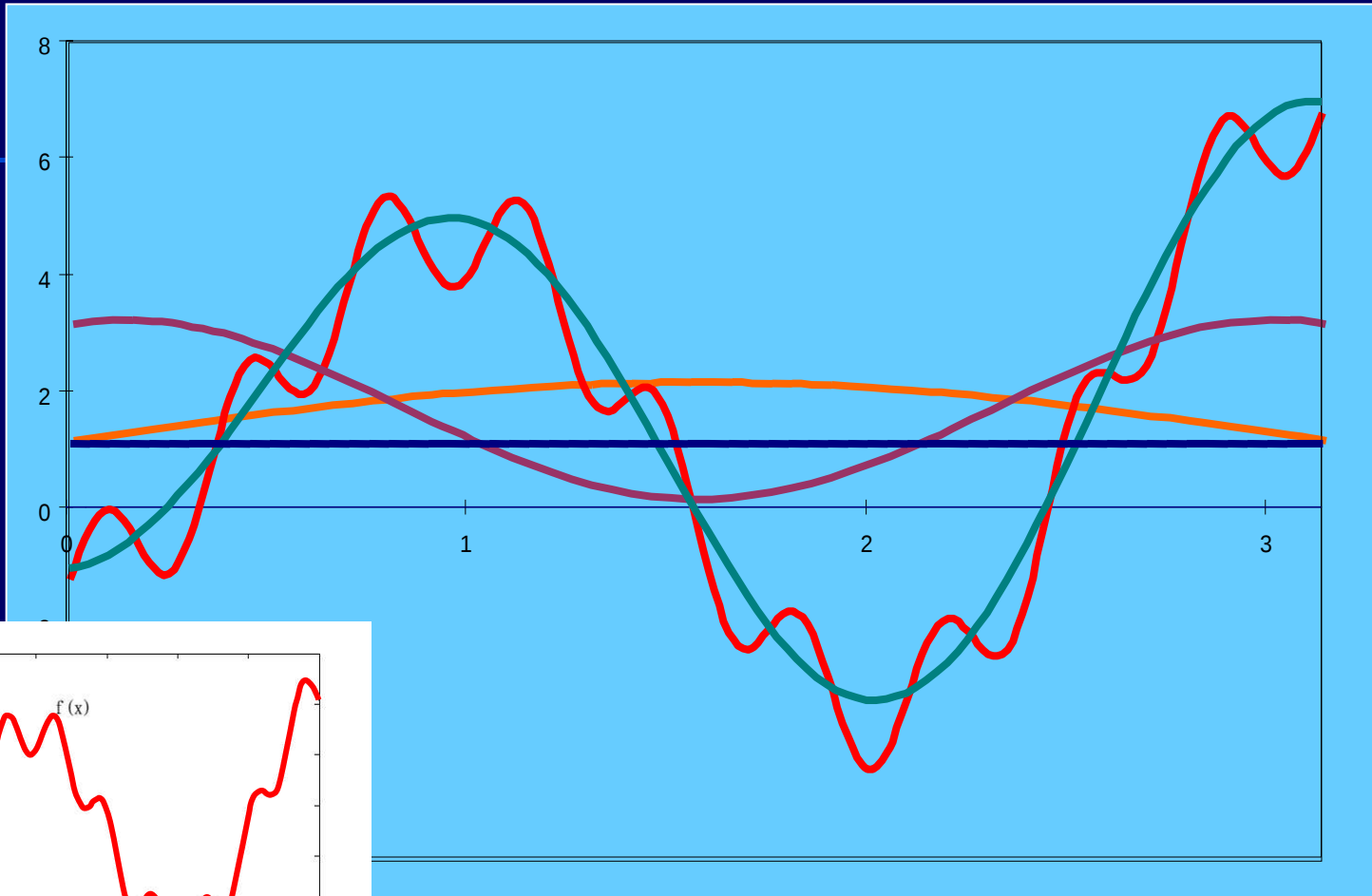
$$f_2(x) = \cos(2x);$$

$$f_3(x) = \cos(3x);$$

$$f_4(x) = \sin(18x);$$



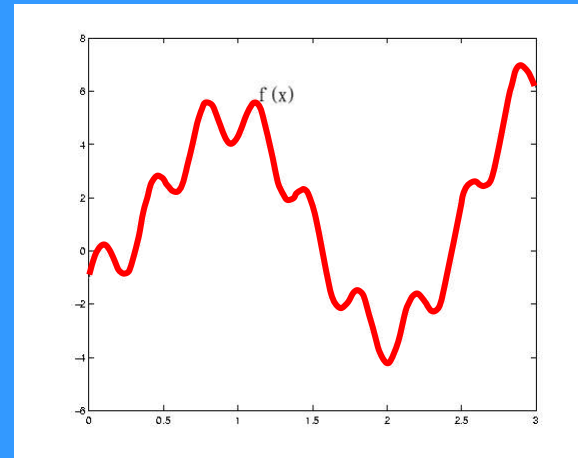
$$f = f_0 + f_1 + 2f_2 - 4f_3 + f_4$$



Wave Transform 波变换

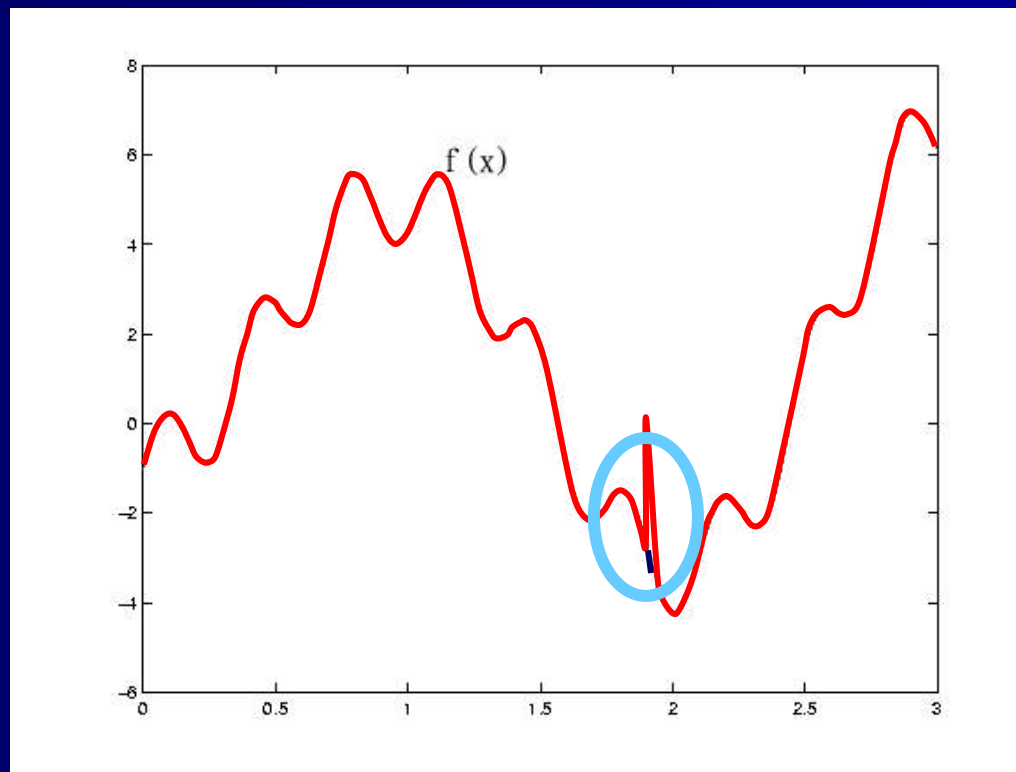
Spectrum

$F(\omega)$



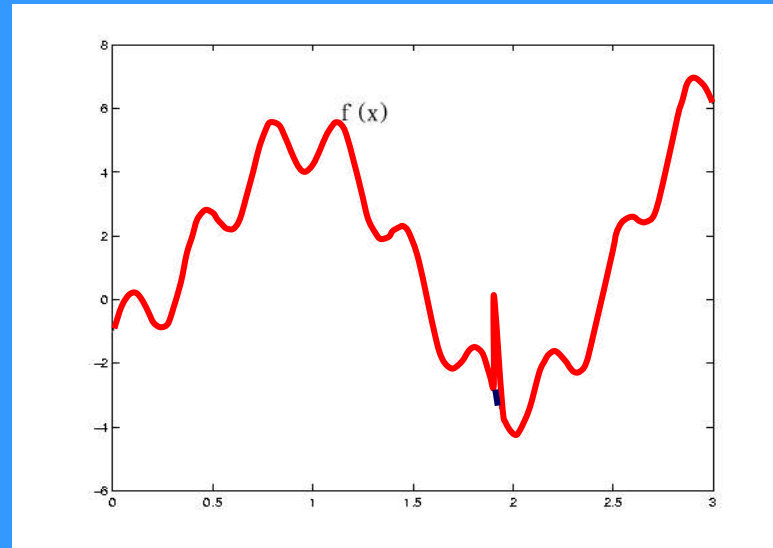
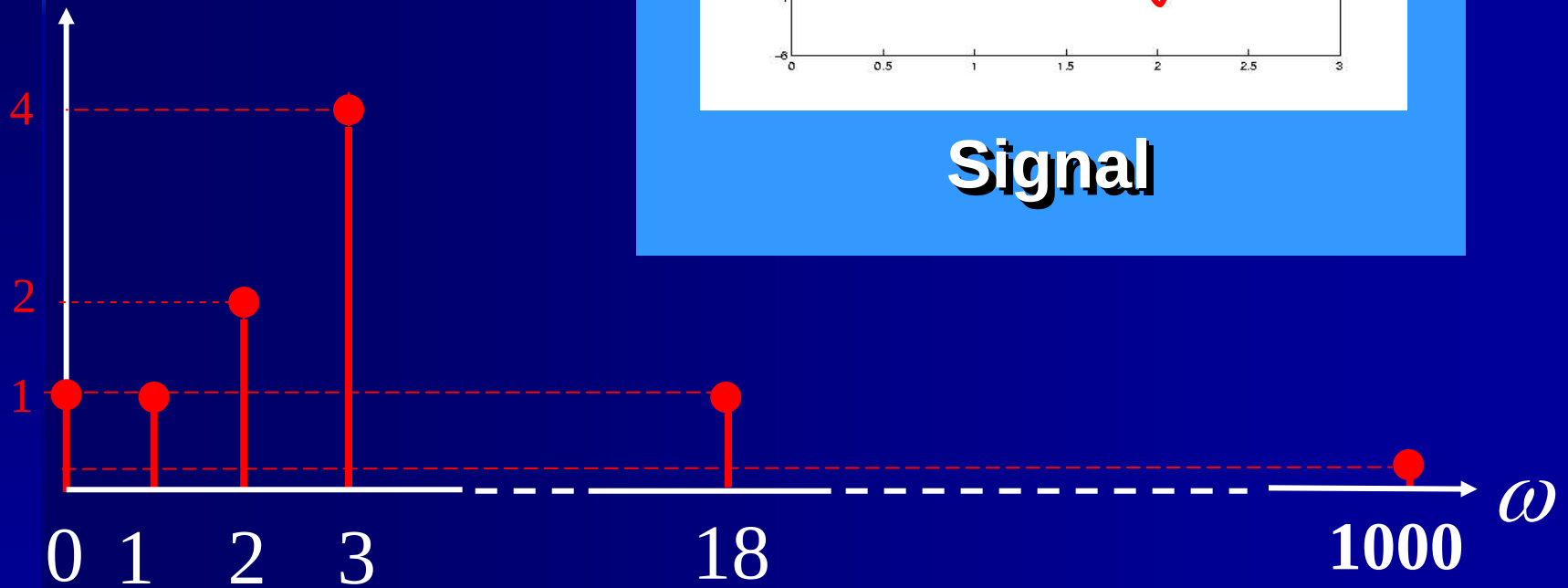
Signal

Fourier analysis, based on analyzing global frequency distribution of a signal, can not characterize the **local behavior** of the signal

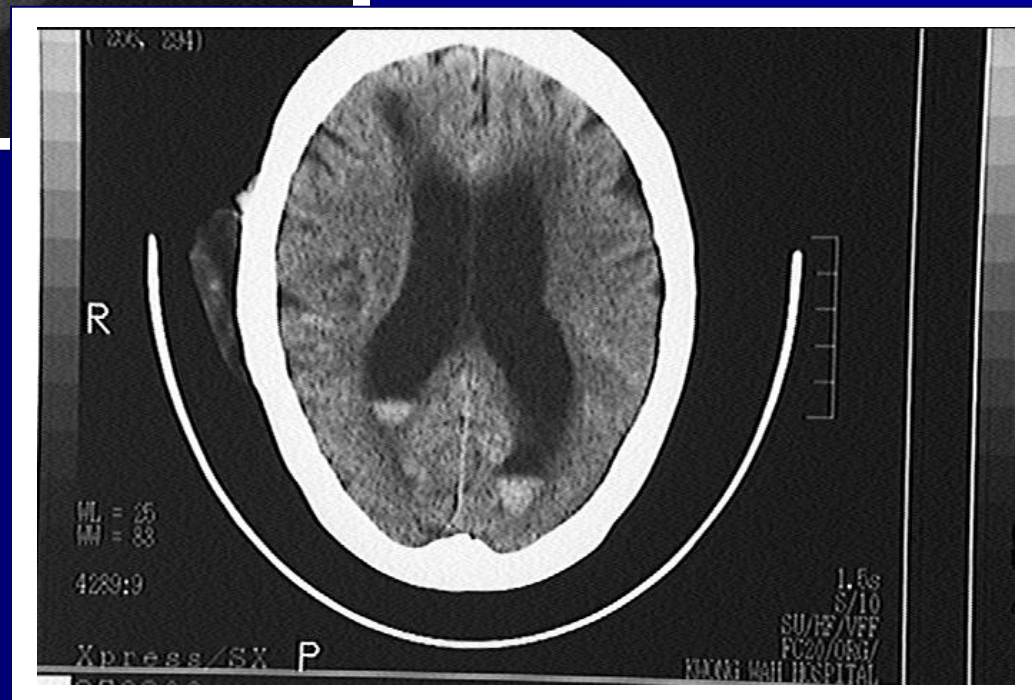
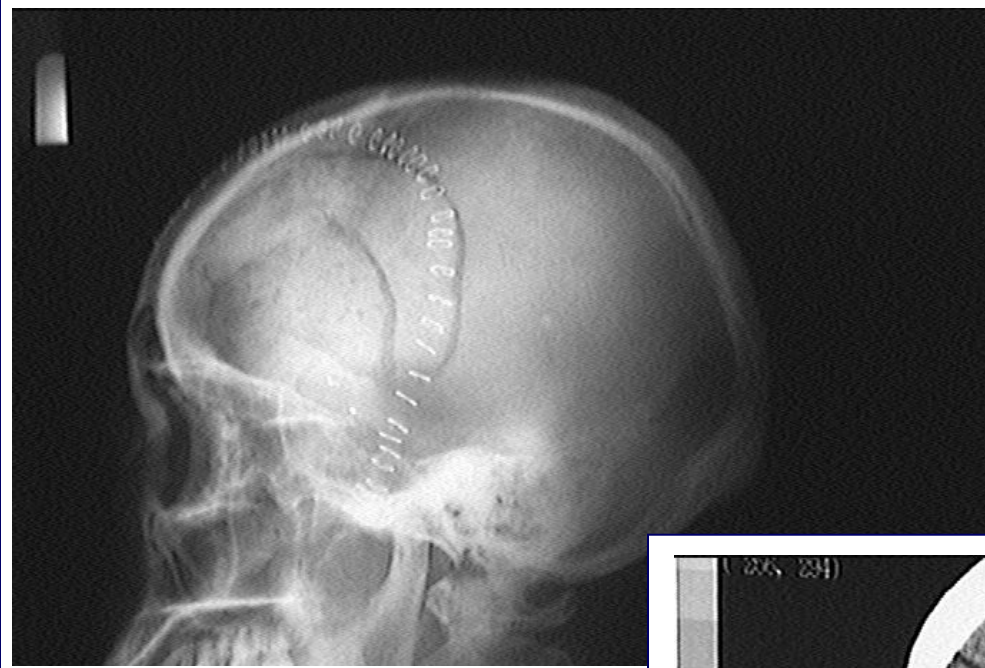


Spectrum

$F(\omega)$



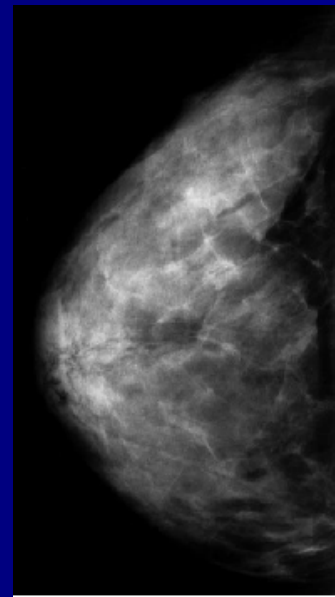
Signal



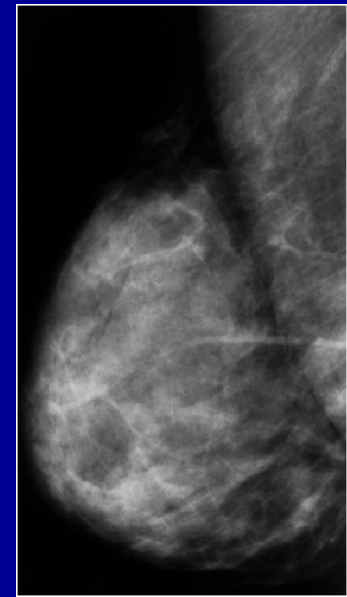
Detection of Breast Cancer using Mammography



Mammography



CC view



MLO view

Mammograms

High Risk of Breast Cancer

Estimated new breast cancer cases and deaths in women by age, United States, 1999

Age	In Situ	%	Invasive	%	Deaths	%
<30	100	0.3	800	0.5	100	0.2
30-39	1,400	3.5	7,400	4.2	1,200	2.8
40-49	9,000	22.6	32,100	18.3	5,600	12.9
50-59	10,000	25.1	37,400	21.4	7,000	16.2
60-69	8,500	21.3	32,600	18.6	7,100	16.4
70-79	8,200	20.6	40,700	23.2	11,000	25.4
80+	2,700	6.8	24,000	13.7	11,300	26.1
Total	39,900	100.0	175,000	100.0	43,300	100.0

Due to rounding, percentages may not exactly total 100%.

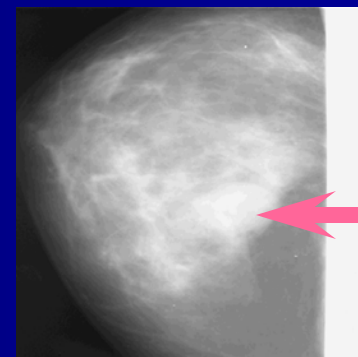
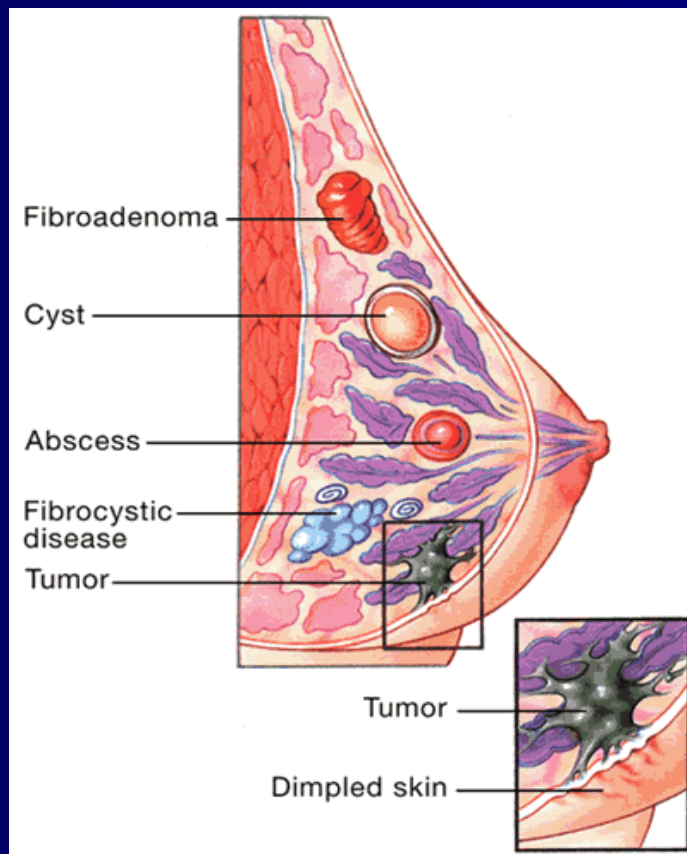
American Cancer Society, Surveillance Research, 1999.

Expected survival rates for women diagnosed with breast cancer

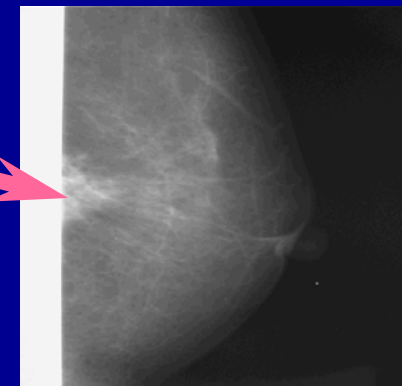
- **85 % five years after diagnosis**
 - 43% for leukemia
 - 14% for lung cancer
- **71 % after 10 years**
- **57 % after 15 years**
- **52 % after 20 years**

Breast Cancer Facts & Figures 1999-2000
American Cancer Society

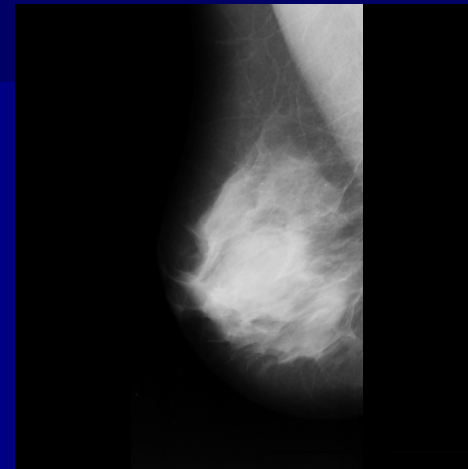
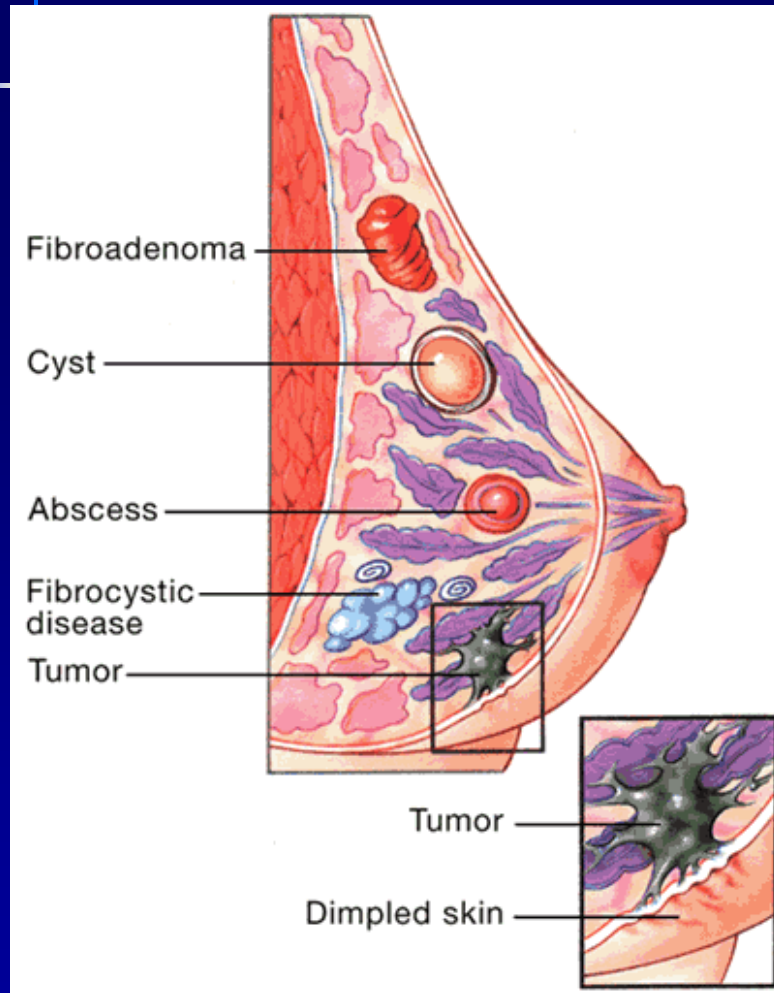
Lesions: Masses or Microcalcifications



Microcalcifications

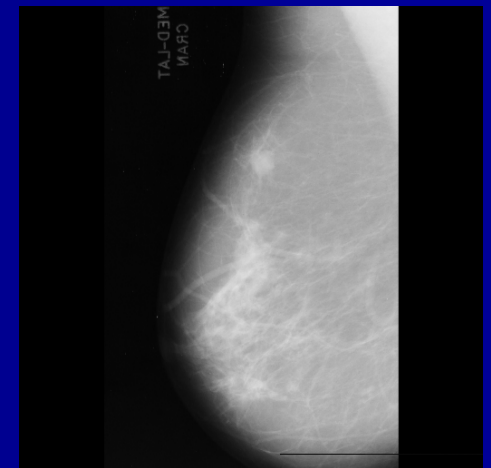


Tumors: Benign or Malignant



Benign

Malignant



函数 $\psi(t) \in R$ 小波函数, 在 $L^2(R)$ 空间, 小波变换为

$$(W_{\psi} f)(a, b) = \frac{1}{\sqrt{a}} \int_R f(t) \psi\left(\frac{t-b}{a}\right) dt,$$

其中

a 是频率参数, b 是时间参数.

Wavelet
Transform
小波变换

1986年

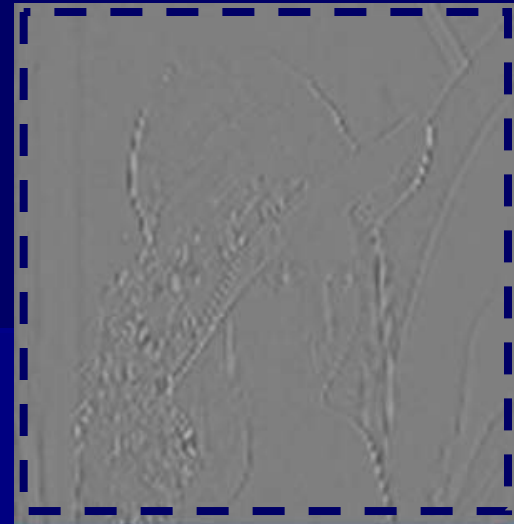
Wave Transform
波变换

1822年

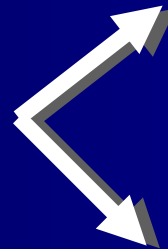
$$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-j\omega t} dt$$

ω 是频率参数

$$V_j = V_{j+1} \oplus W_{j+1}$$



高频

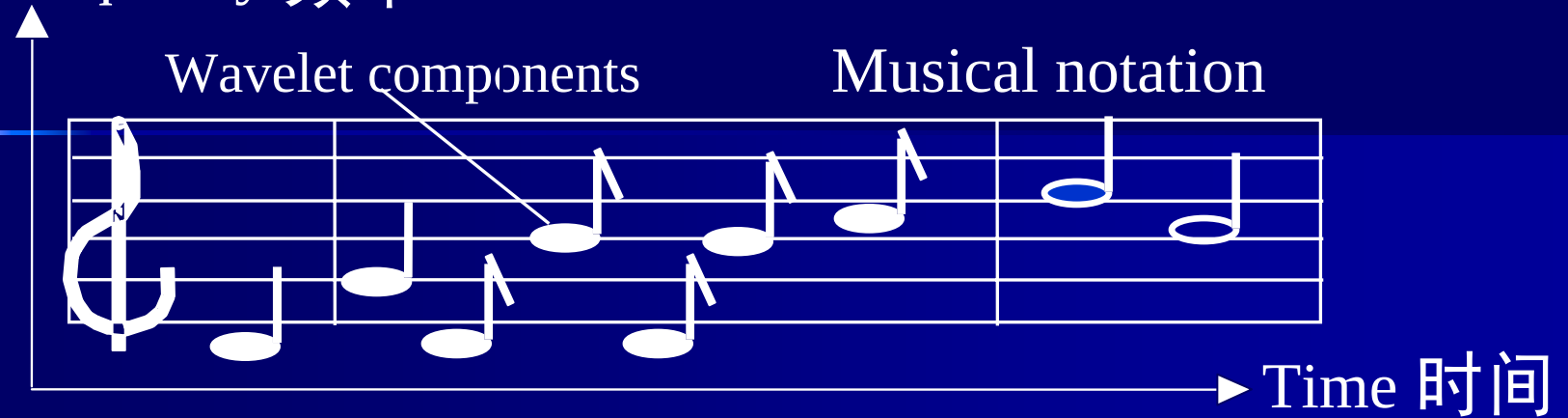


低频

Wavelet Transform 小波变换

小波变换产生音乐乐谱

Frequency 频率



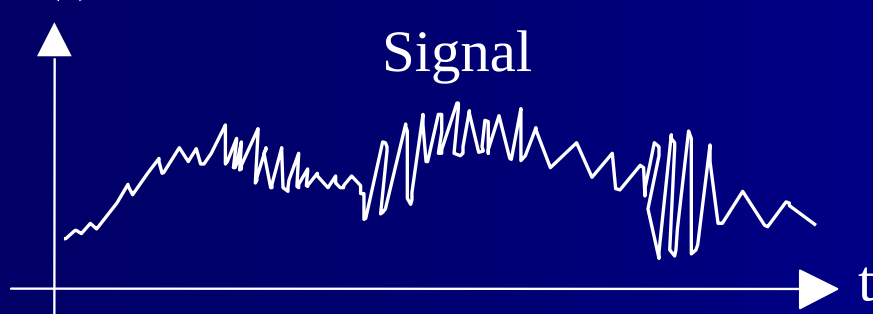
Wavelet
transform



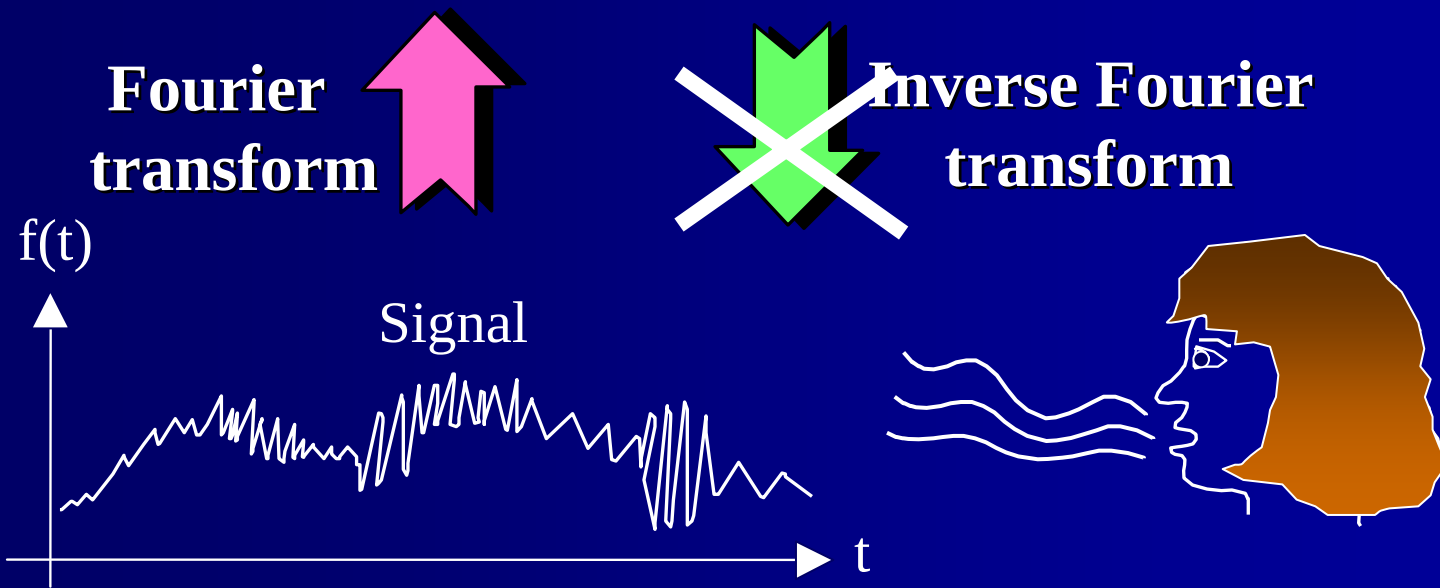
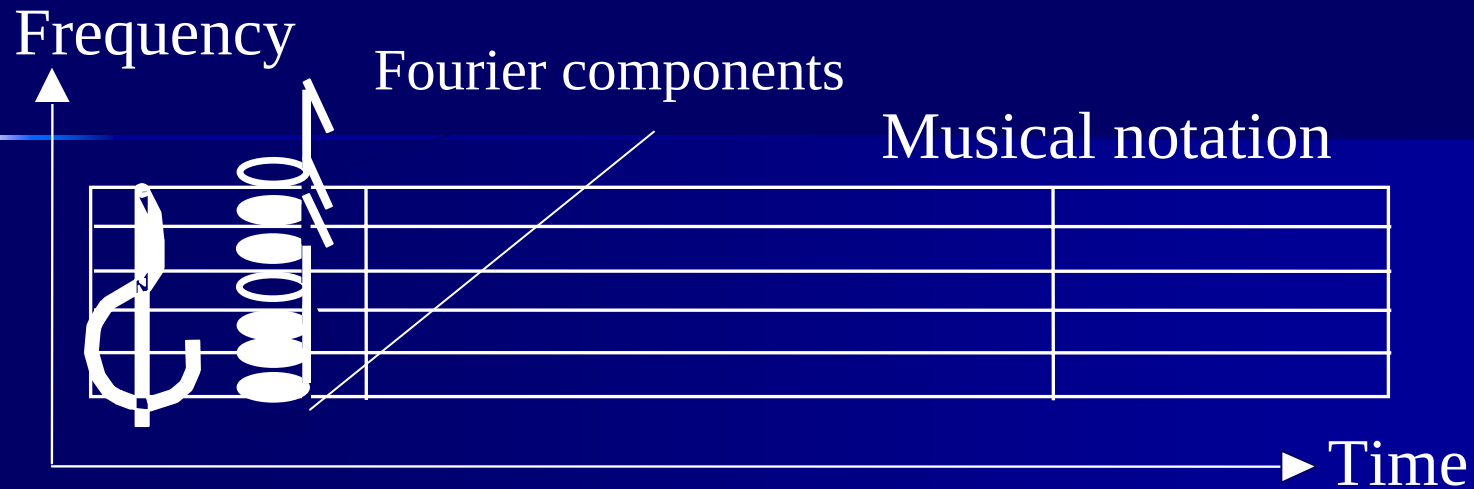
Inverse wavelet
transform



$f(t)$



波变换不能产生音乐乐谱



多分辨分析 (MRA)

一个在 $L^2(\mathbb{R})$ 空间的闭子空间系列 $\{V_j\}_{j \in \mathbb{Z}}$ 如果满足以下条件，就称为多分辨分析 MRA:

1 $V_j \subseteq V_{j-1}$ for any $j \in \mathbb{Z}$

2 $\text{clos}_{L^2(\mathbb{R})}(\cup V_j) = L^2(\mathbb{R})$, $\cap V_j = \{0\}$

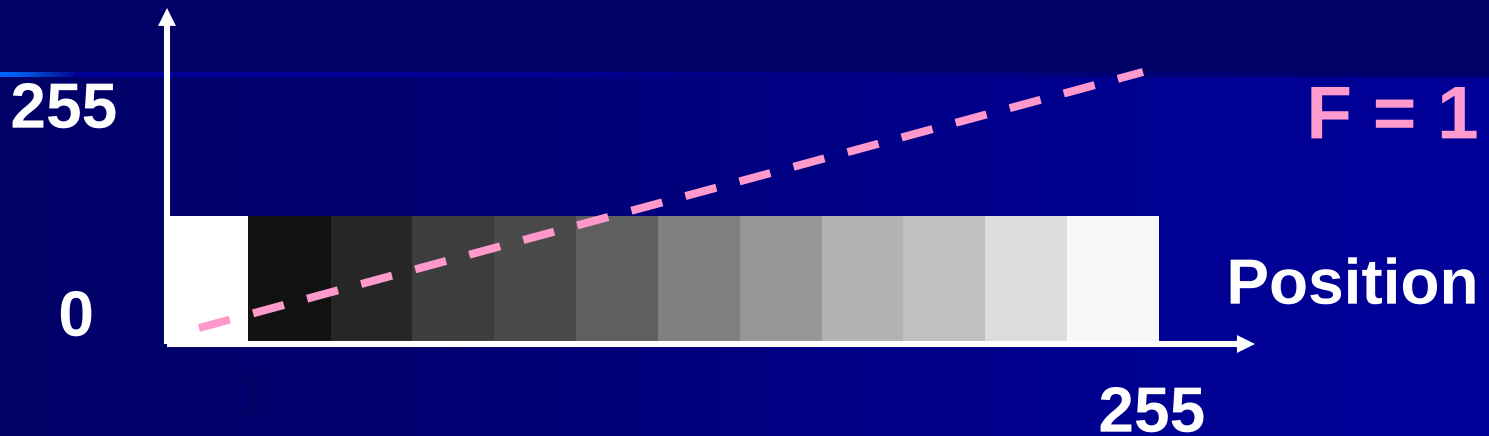
3 $u(x) \in V_j \Leftrightarrow u(2x) \in V_{j-1}$

4 $u(x) \in V_0 \Leftrightarrow u(x-k) \in V_0$

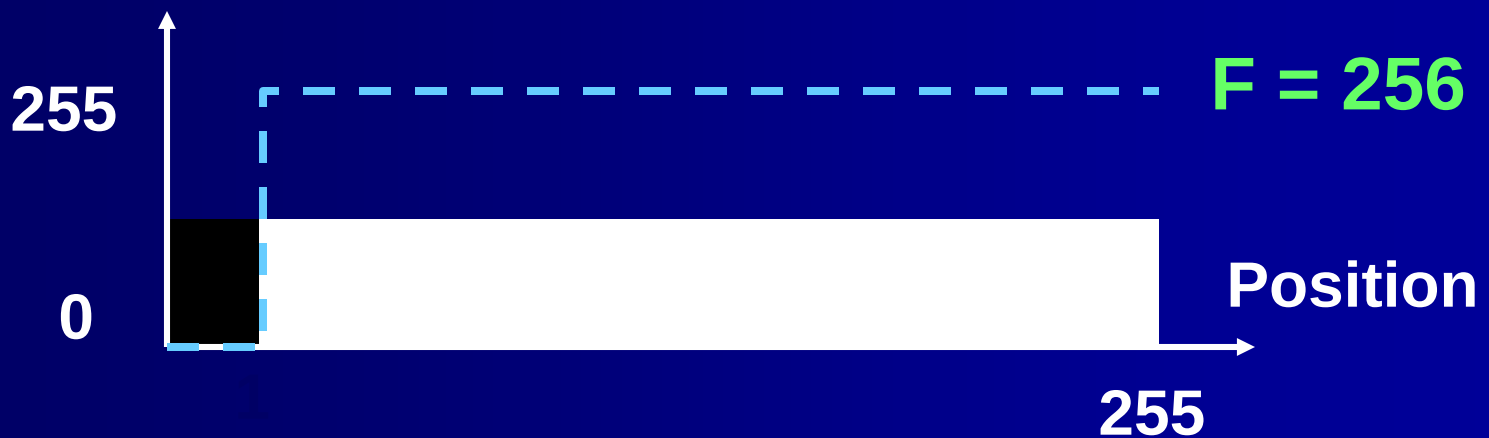
5 存在一个生成函数 $g(x) \in V_0$ 它可以构成闭子空间 V_0 的 Riesz 基

图像灰度的变化频率

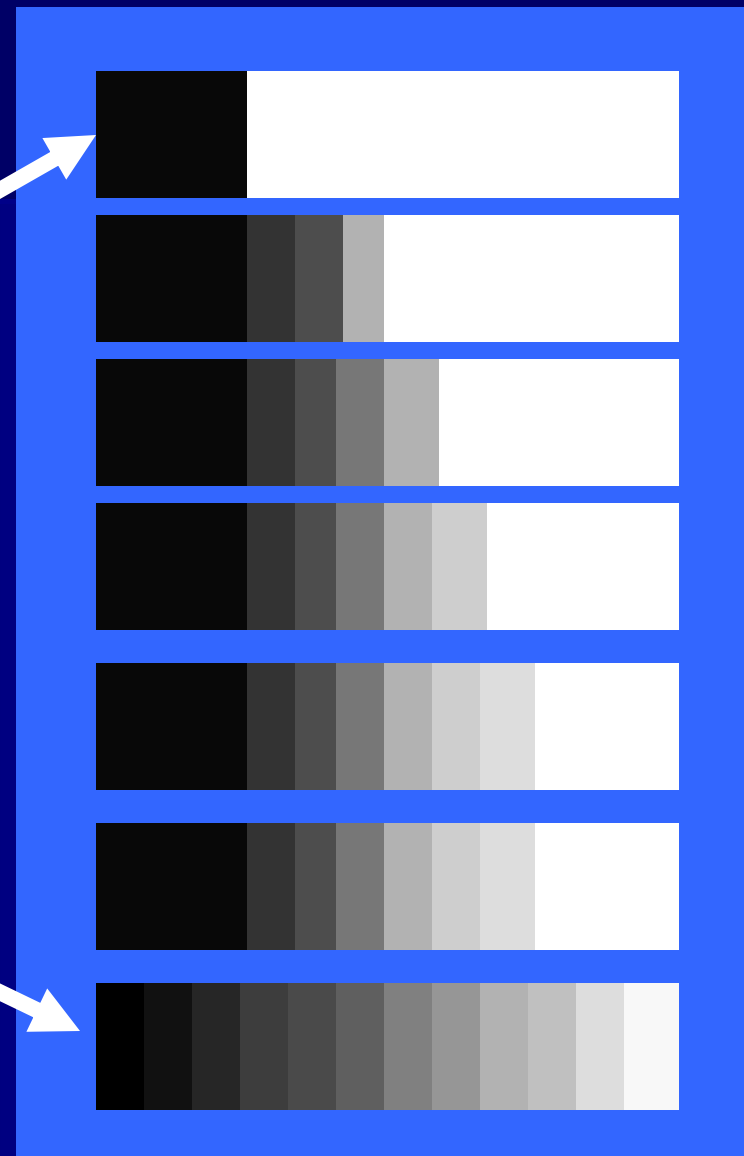
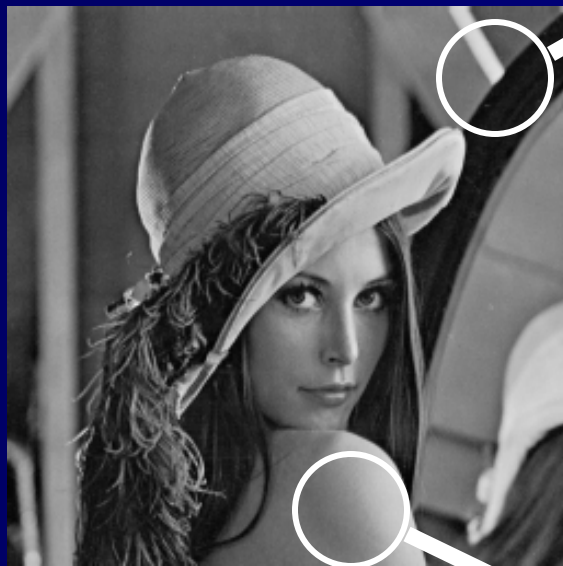
Grey level

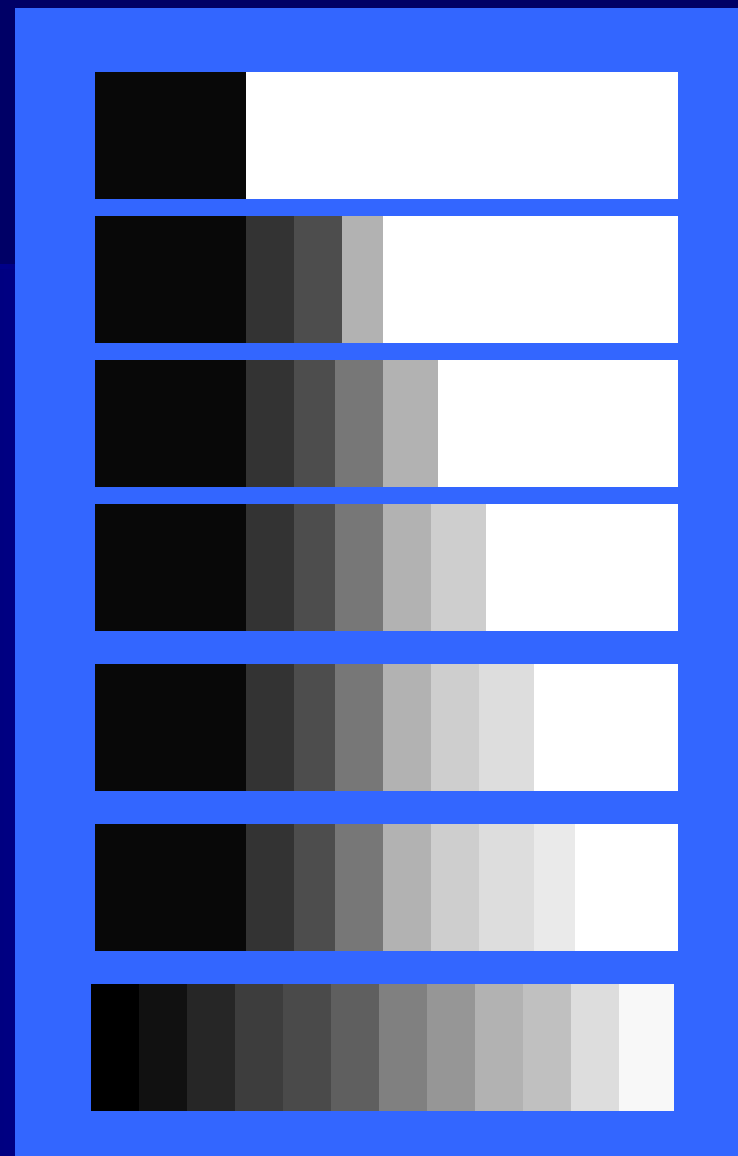


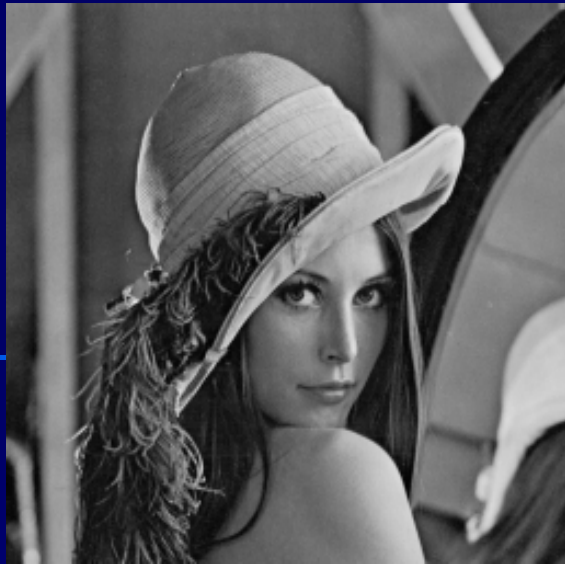
Grey level



任何一个图像 $f(x,y)$ 都属于某个闭子空间 V_j



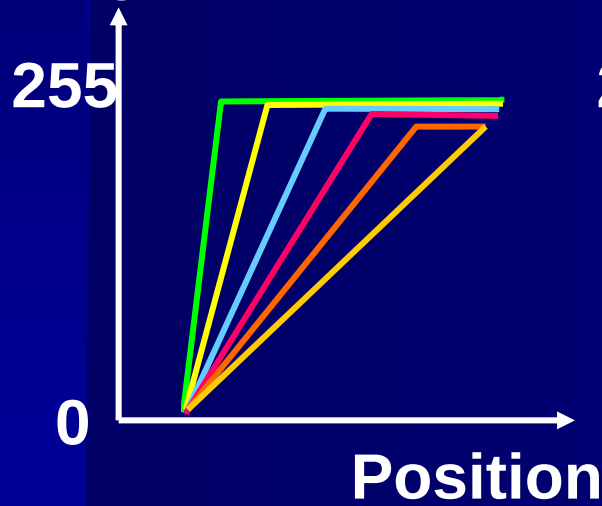



 V_j

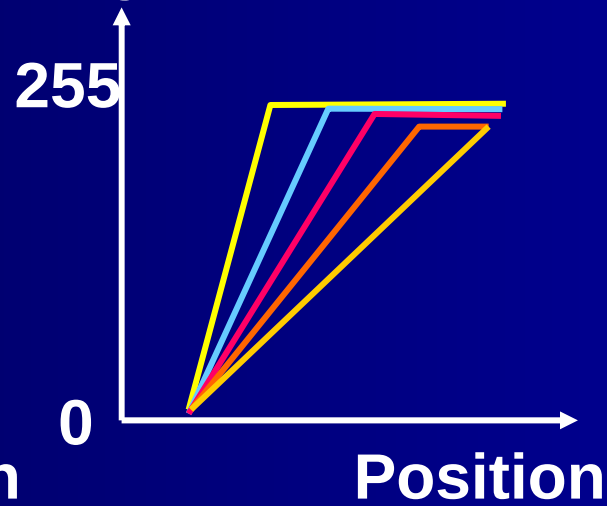
 V_{j+1}

 V_{j+2}

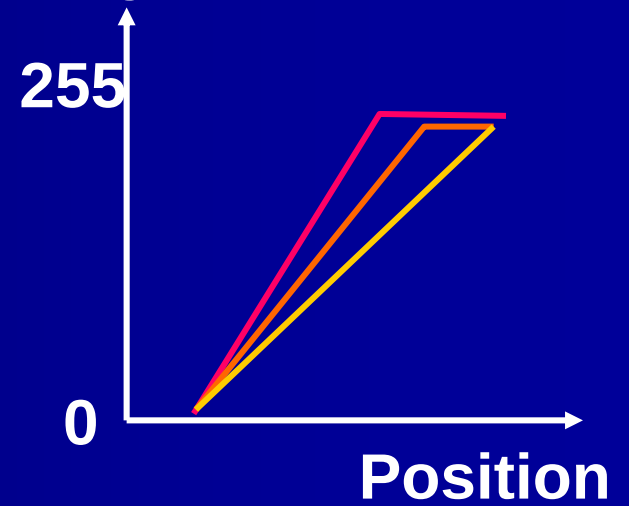
Grey level



Grey level

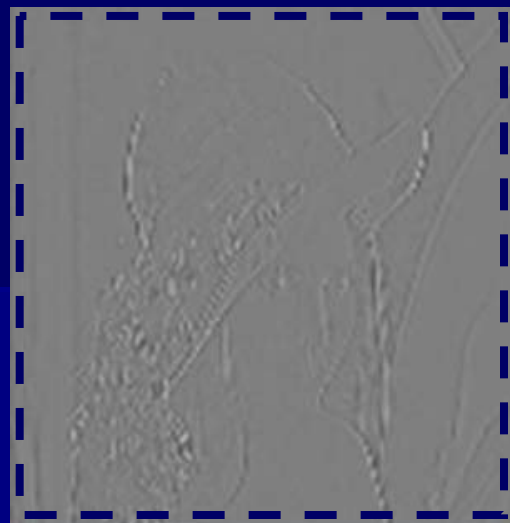
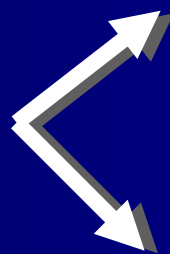


Grey level



$$\dots V_{j+2} \subset V_{j+1} \subset V_j$$

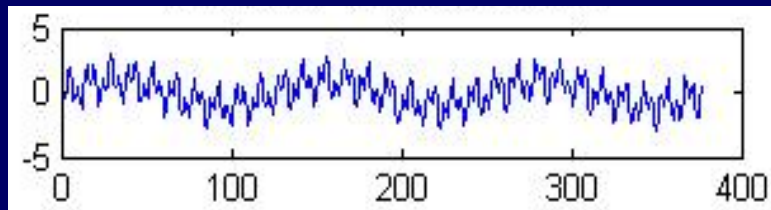
$$V_j = V_{j+1} \oplus W_{j+1}$$



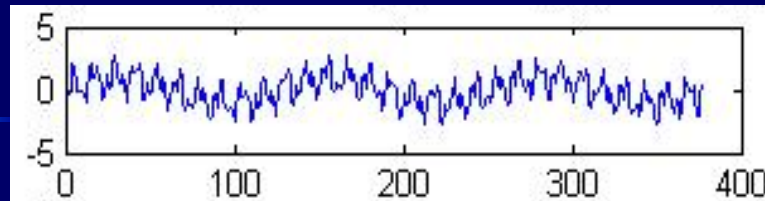
高频



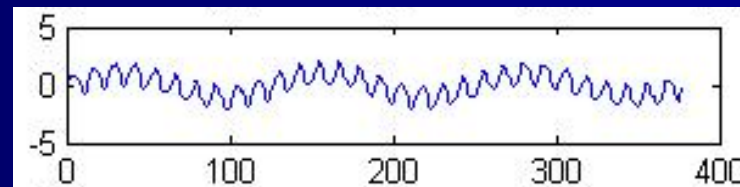
低频



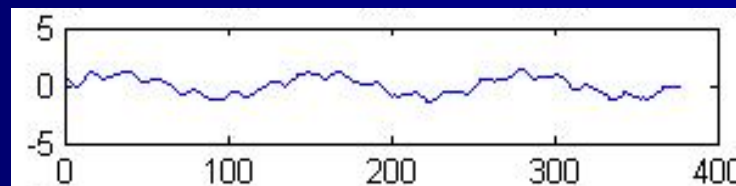
V_j



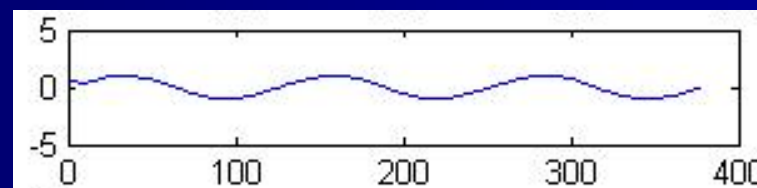
V_{j+1}



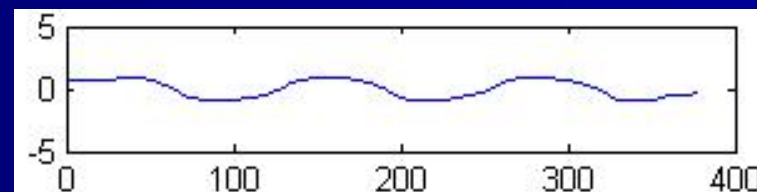
V_{j+2}



V_{j+3}



V_{j+4}



V_{j+5}

$\dots V_{j+2} \subset V_{j+1} \subset V_j$

$$V_j = W_{j+1} \oplus V_{j+1}$$

↓

$$(W_{j+2} \oplus V_{j+2})$$

↓

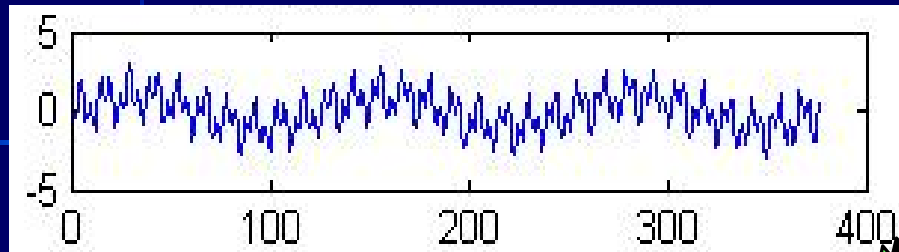
$$(W_{j+3} \oplus V_{j+3})$$

...

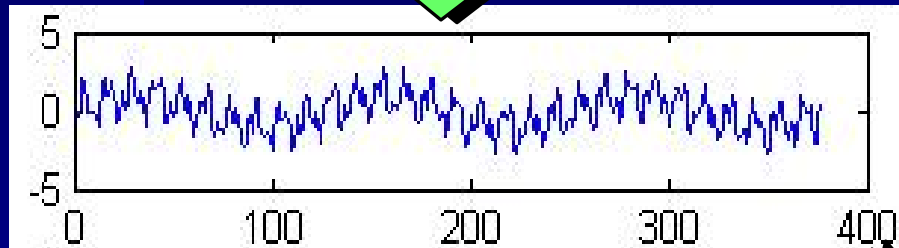
V_j

W_{j+1}

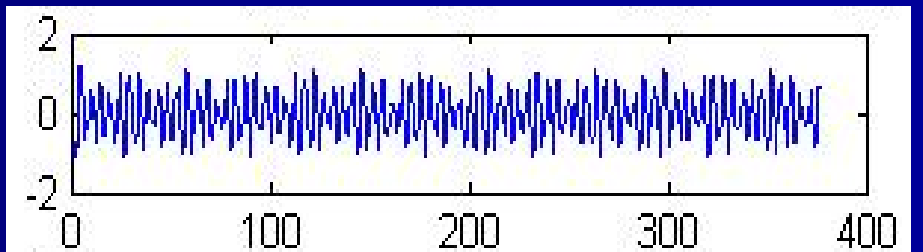
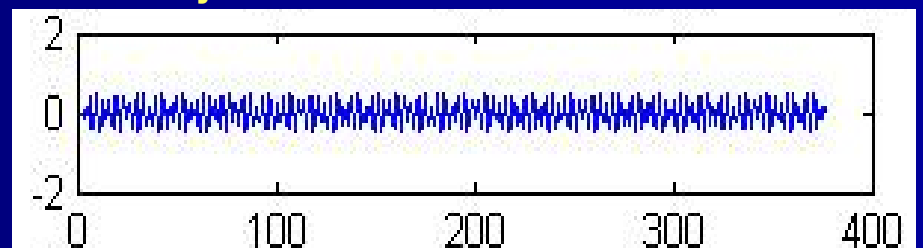
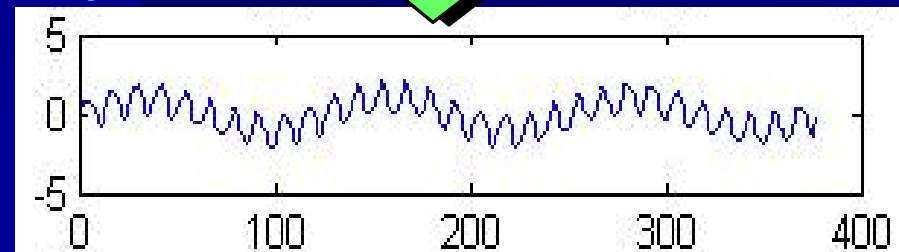
W_{j+2}



V_{j+1}

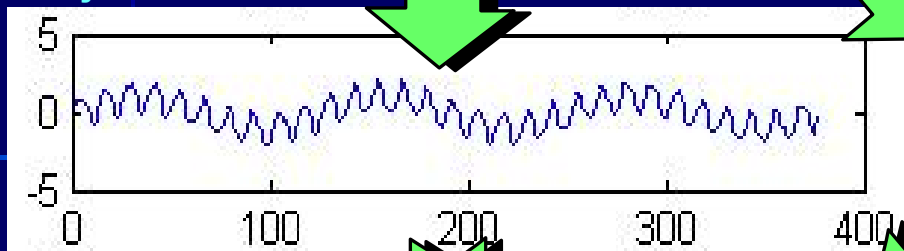


V_{j+2}

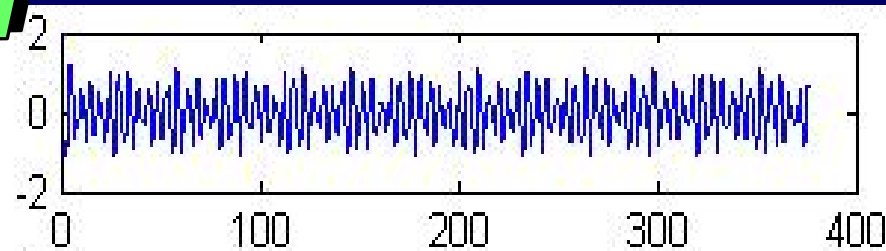


V_{j+2}

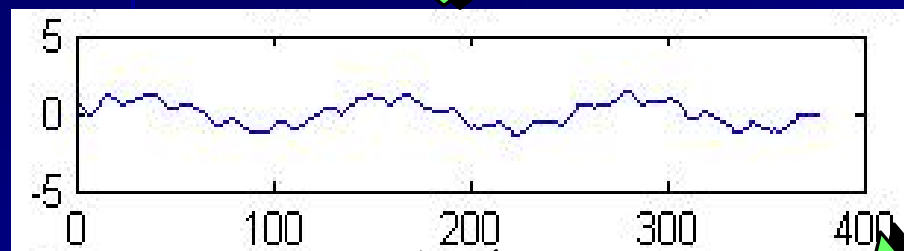
V_{j+1}



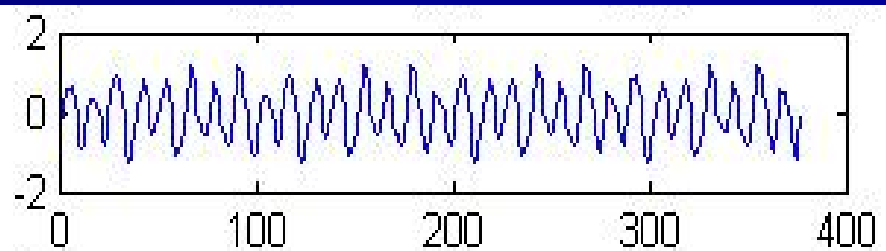
W_{j+2}



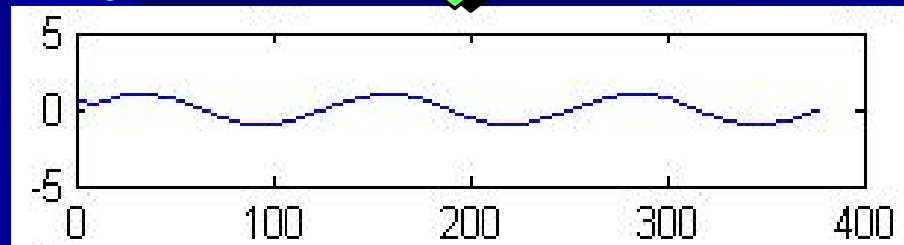
V_{j+3}



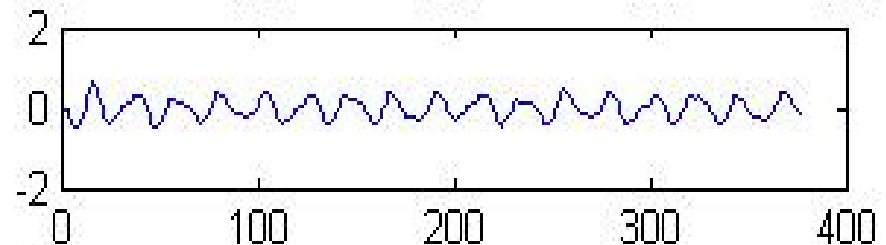
W_{j+3}



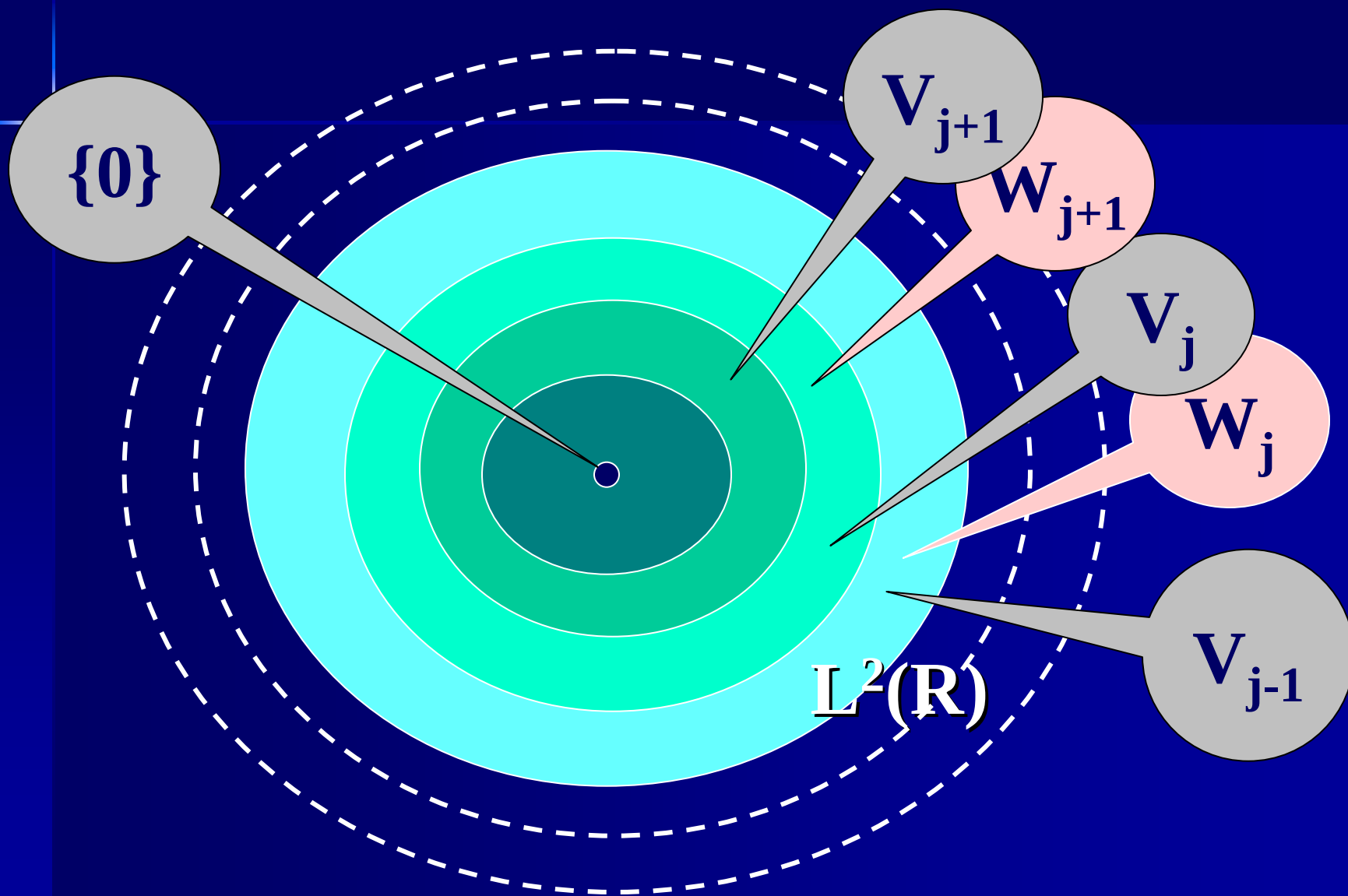
V_{j+4}



W_{j+4}



多分辨率分析中的闭子空间



希尔伯特空间理论应用到 图象传输

**A Wavelet-based Progressive Digital Image
Transmission Scheme**

基于小波的累进图象传输(PIT)

Chin-Chen Chang,

Tzu-Chuen Lu

National Chung Cheng University

图象传输



Sender



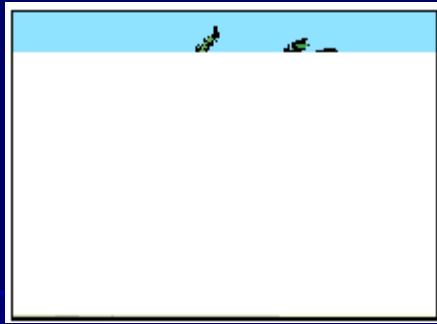
Internet



Receiver



First Phase



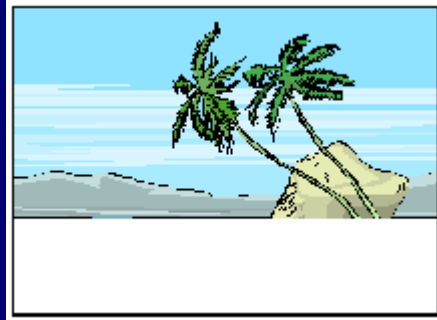
Second Phase



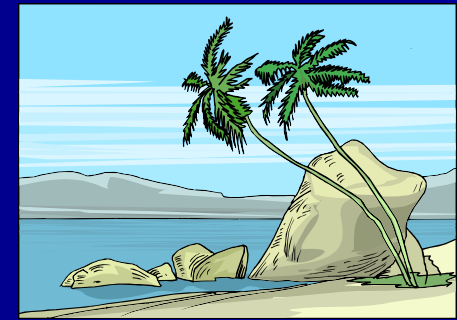
Third Phase



Fourth Phase



Fifth Phase



Sixth Phase



基于小波的累进图象传输(PIT)



First Phase



Second Phase



Third Phase



Fourth Phase



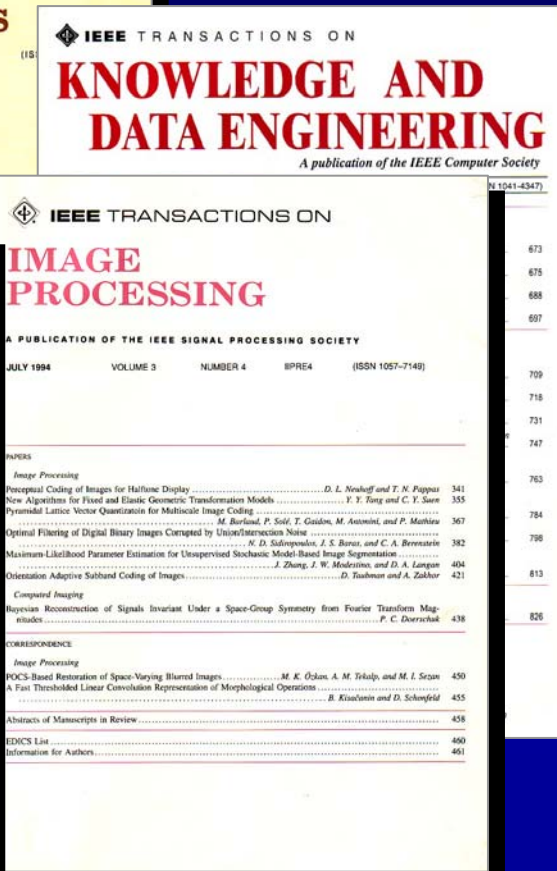
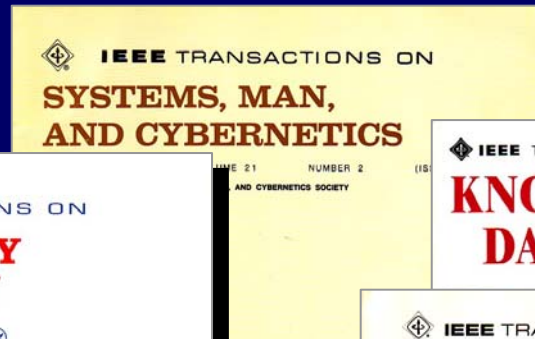
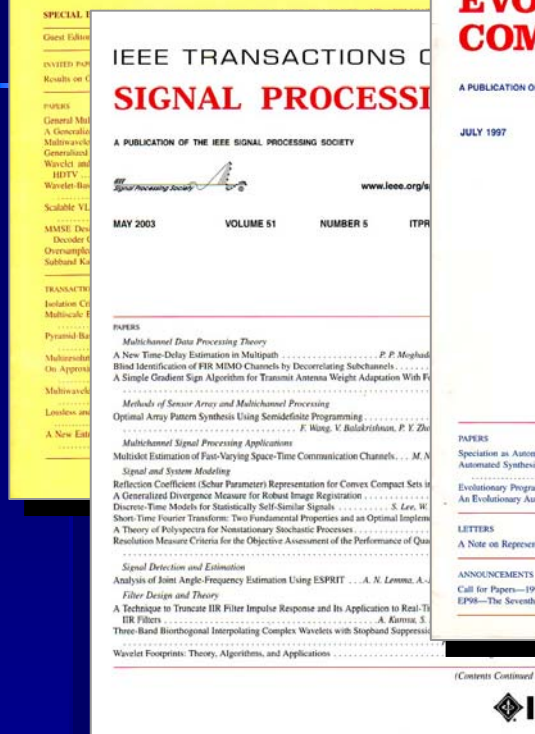
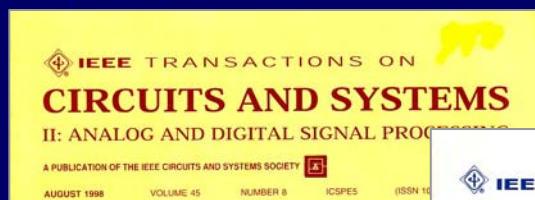
Fifth Phase



Sixth Phase

希尔伯特空间理论应用到 模式识别、文本分析领域

- ◆ 文本分析的**非层次理论**
- ◆ **基于小波**的文本分析理论

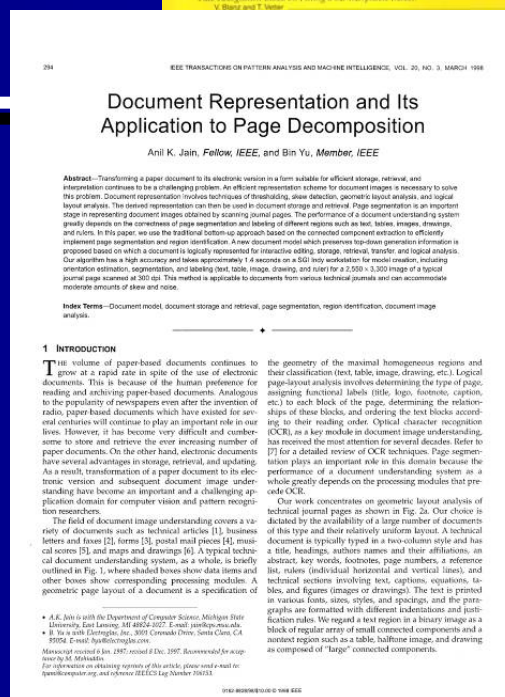
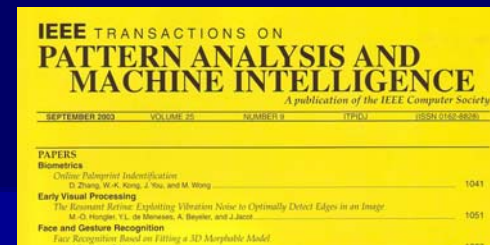


在国际一流的IEEE期刊、其他国际权威的期刊和重要的国际会议上发表论文



美国A.K. Jain教授对将
《非层次理论》列为国
际上目前公认的文本分
析重要算法，给予了肯
定评价：

国际著名模式识别专家、原IEEE
Trans. on Pattern Analysis and
Machine Intelligence主编、美国
Michigan大学的 A. K. Jain教授
在IEEE Trans PAMI的带总结性
的论文中[1]，称这些理论“解
决了高复杂度几何结构的文本分
析问题”。



[1] IEEE Trans PAMI, 1998,
Vol. 20(3):294-307, (评价
处为第296,297页)



国际著名模式识别专家
George Nagy 在国际权威的
IEEE PAMI总结性的论文
《文本图像分析20年》[2]
中, 对我们的工作给予了高
度评价:

“**论文[82]**提出了一个基于数据而不是基于模型的方法来去掉表格线条。它的创新点不在于如何去掉表格文本中的那些水平和垂直线条, 而在于**打破了那些墨守成规的方法**, 应用了二维多分辨率小波分析 (MRA)。实验的结果被**三种金融文本所论证**, 正如作者所述, 这种新方法展示了完美的性能。”

[2] IEEE Trans PAMI, 2000, 22(1):38-62,
公开评价处为第296,297页

[82] IEEE Trans PAMI, 1997,
19(8):921-926



评价唐远炎的论文



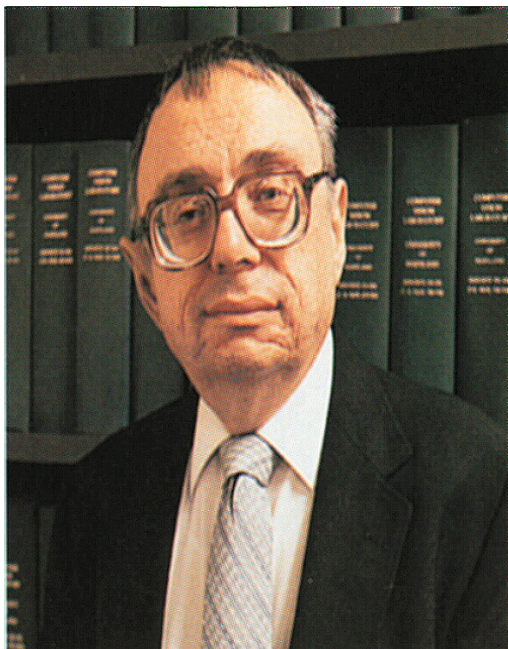
国际著名模式识别专家、美国Drexel大学、IMPACT 主任 Meystel教授对“小波-文本分析理论”的高度评价[3]

“基于小波变换的理论...可能被下面的问题所困扰：大多数小波变换对不同解析层次的表示处理趋于相似的功效。另外一个重要的不足：每个层次处理的精度经常应该是一样的。这样它没有导致希望的在各种情况下复杂度下降。然而，[25]的最新研究成果解决了上述问题。”

[25] IEEE Trans PAMI, 1997, Vol. 19(8):921-926



[3] IEEE Trans SMC(C),
2003, Vol. 33(1):86-101, 公
开评价处为第92页



SURVEY

Image Analysis and Computer Vision: 1999¹

Azriel Rosenfeld

Computer Vision Laboratory, Center for Automation Research, University of Maryland,

College Park, Maryland 20742-3275

Received January 10, 2000

This paper presents a bibliography of nearly 1,000 references relating to computer vision and image analysis, arranged alphabetically. The topics covered include: computational techniques; feature detection and segmentation; image and scene analysis; two-dimensional shape; pattern recognition; three-dimensional shape; and motion. A few references are also given on related topics: image processing, sensors and optics; visual perception; neural networks; artificial intelligence; and applications. © 2000 Academic Press

[28] Wavelet Theory and its Application to Pattern Recognition, World Scientific, Singapore, 1999.

[29] Advances in Oriental Document Analysis and Recognition Techniques, World Scientific, Singapore, 1999.

[30] IEEE Trans. PAMI 21(6):544–551, 1999

原美国总统计算机视觉科学顾问组主席A.Rosenfeld在他的综述《图像分析与计算机视觉》[4]中，将我们的两本专著和一篇论文[28–30]中的5项成果列为国际上该领域主要的研究成果之一。

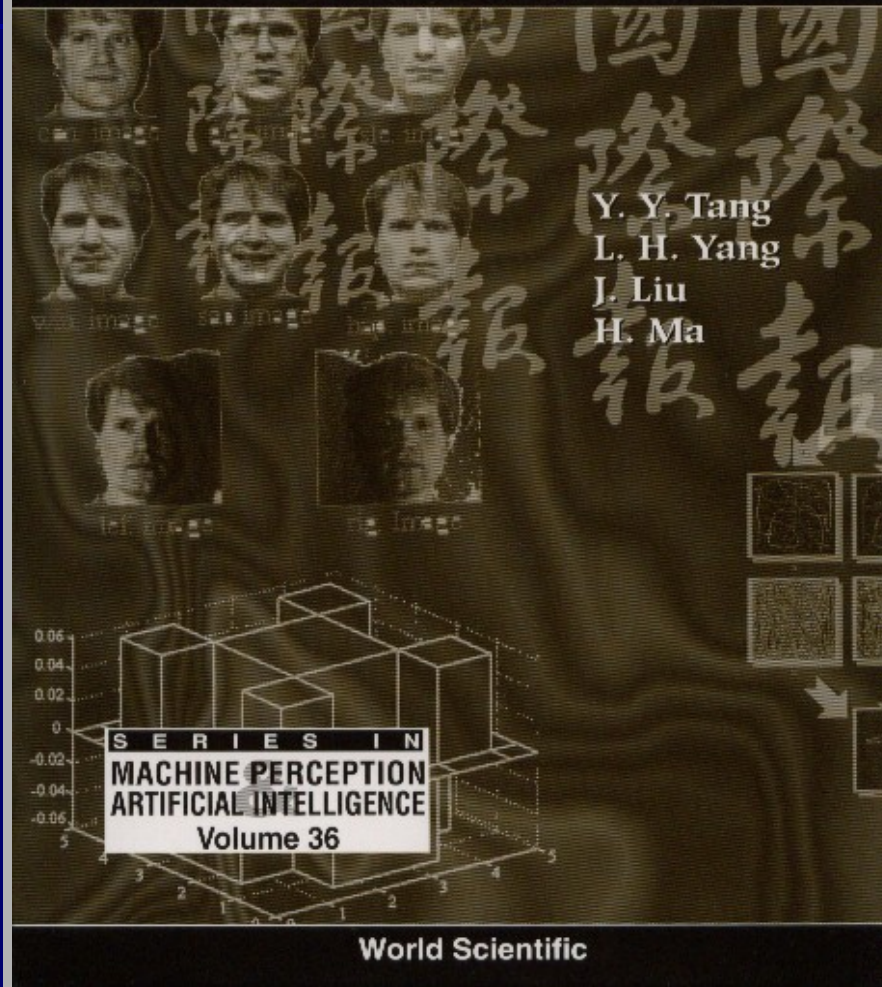
INTRODUCTION

bibliographies on computer processing of published during 1999. (The online availability makes it increasingly unnecessary to publish almost entirely to a selected set of U.S. editions. No attempt is made to summarize only to provide a convenient compendium of the following headings:

Grant N00014-95-1-0521 is gratefully acknowledged, as

[4] Computer Vision and Image Understanding, 1999, 78:222–302, 公开评价处为第223, 224, 230, 253页

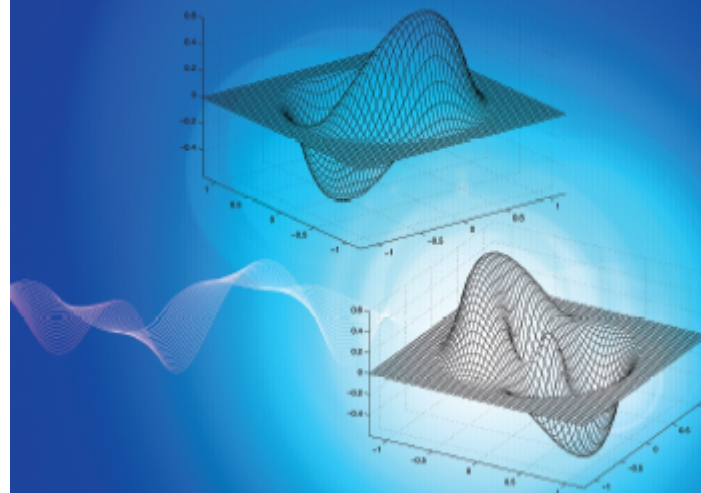
Wavelet Theory and Its Application to Pattern Recognition



WAVELET THEORY APPROACH TO PATTERN RECOGNITION

2nd Edition

Yuan Yan Tang



 World Scientific

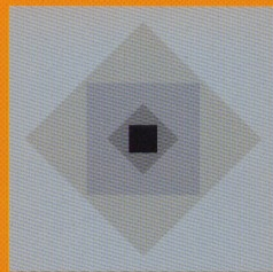
SERIES IN
MACHINE PERCEPTION
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Volume 74

现代应用数学方法丛书 ⑨

21
数学天元基金

小波分析与文本文字识别

唐远炎 王 玲 著



科学出版社
www.sciencep.com

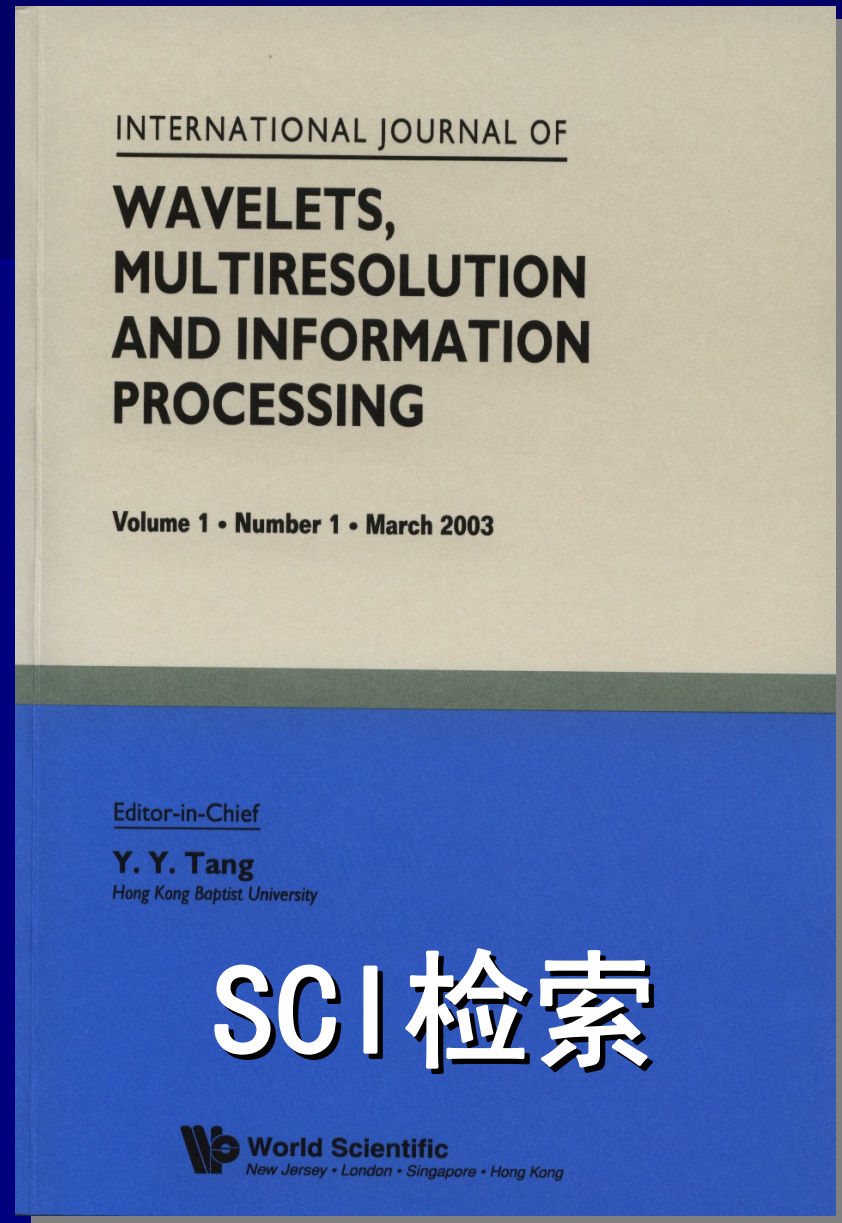
<http://www.worldscinet.com/ijwmip/ijwmip.shtml>

**SCI Indexed
Journal**

**International
Journal of
Wavelets,
Multiresolution
and Information
Processing**

**Editor-in Chief
Y. Y. Tang**

yytang@comp.hkbu.edu.hk



计算机科学前沿

主编：李未

执行主编：陆汝铃

副主编：陈国良，赵沁平，
唐远炎

是教育部发起，高等教育出版社主办，Springer负责全球发行的Frontiers in China英文系列期刊中的一个分册。内容上希望既能反映国际国内研究热点、前沿，同时具有中国自主创新特色。将对计算机学科的发展起重要的作用。

EI检索



2007年创刊

IEEE系列国际学术会议

International Conference on Wavelets Analysis and Pattern Recognition (ICWAPR)

EI检索

yytang@comp.hkbu.edu.hk

International Conference on Wavelet Analysis and Pattern Recognition 2010

Qingdao, Shangdong, China 11 - 14 July 2010

<http://www.icwapr.org>

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Preliminary Call for Papers

ICWAPR 2010 will be held on 11 - 14 July 2009 in Qingdao, Shangdong, China. This is the eighth conference of its kind on the subject of wavelet theory and its applications. The conference aims to bring together researchers in wavelet analysis and pattern recognition to explore the synergy in combining these closely related areas of study. This conference will build on our past experiences and network to provide a valuable forum for exchanges of significant ideas and publication of research results in these areas. The conference offers opportunity for selected works to be published first in the conference proceedings and possibly later in special issue of journals. The multiple themes and topics of interest include, but are not limited to:

Wavelet Analysis:

- General Theory
- Bases and Frames Theory
- Wavelets and Filter Banks
- Wavelet and Sampling
- Approximation Theory
- Spline Theory
- Equation
- Time-Frequency Analysis
- Integral Transforms
- Wavelet and Statistics
- Wavelet and Differential and Integral Equations
- Wavelet and Numerical Analysis
- Wavelet and Functional Analysis
- Wavelet Neural Network
- Hardware and Software Implementation of Wavelet Transforms
- Algorithms

Pattern Recognition & Related Fields:

- Visualization
- Watermarking
- Biometrics
- Signal Estimation
- Image Fusion
- Image Recovery
- Image Compression
- Segmentation
- Biomedical Imaging
- Document Analysis
- Learning Theory
- Noise Reduction
- Machine Vision
- Classification
- Feature Extraction
- Emotion Computation
- Cluster Analysis
- Deformation Analysis
- Descriptor of Shapes
- Diagnosis of Faults
- Intelligent Robot
- Medical Image Analysis
- Human Face Recognition
- Hand Gestures Classification
- Iris Pattern Recognition
- Invariant Representation of Patterns
- Image Indexing and Retrieval
- Range Imaging and Detection
- Seismological Signal Processing
- Stochastic Pattern Recognition
- Texture Analysis and Classification
- Animation Image Analysis
- Enhancement and Restoration
- Nonstationary Stochastic Processing
- Handwritten and Printed Character Recognition
- Analysis and Detection of Singularities
- Artificial Life
- Intelligent Control System
- Intelligent Human Machine Interface
- Information Safety

Submission Guidelines

Prospective authors should prepare a full paper and submit it on line through our website in PDF format. Each paper should not exceed 6 pages in A4 format. All papers should conform to the style guidelines outlined on the ICWAPR'09 website. All submissions must be original and have not been submitted to any other publications. Each paper will be reviewed by 2 referees. The papers should provide sufficient background information and should clearly indicate the original contribution to the subject studied. They should state and discuss the main results and provide adequate references. Paper submission implies that one of the authors will attend the conference if it is accepted.

Important Dates

Paper Submission Due:	1 March 2010
Notification of Paper Acceptance:	15 April 2010
Submission of Camera Ready Manuscripts:	5 May 2010

Publication

All papers will be:
- searchable by IEEE Xplore (<http://ieeexplore.ieee.org/>)
- submitted for indexing to EI Compendex
- Selected papers will be published in: International Journal of Wavelet, Multiresolution & Information Processing (IJWMIP) (SCI Indexed)



谢谢 !

yytang@comp.hkbu.edu.hk

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